

a , \mathbf{a} , A and \mathbf{A} represent scalar, vector, constant, and matrix. \mathbf{A}^T , \mathbf{A}^* , \mathbf{A}^H , \mathbf{A}^{-1} denote the transpose, conjugate, Hermitian, inversion of the complex matrix \mathbf{A} , respectively. The notations $\text{Tr}(\mathbf{A})$, and $|\mathbf{A}|$ indicate trace, and determinant of the complex matrix \mathbf{A} , respectively. $\text{Diag}\{\mathbf{A}\}$ denotes a vector whose elements are the diagonal elements of the matrix \mathbf{A} , and $\text{Blockdiag}\left(\{\mathbf{A}_k\}_{k=1}^K\right)$ is a block diagonal matrix with diagonal sub-matrices of \mathbf{A}_k 's. Furthermore, the i -th row and the j -th column of \mathbf{A} are denoted as $[\mathbf{A}]_{i,:}$ and $[\mathbf{A}]_{:,j}$, respectively, and the element in the i -th row and j -th column is denoted as $[\mathbf{A}]_{i,j}$. The symbols dx , ∂x , and df represent the differential, partial differential, and total differential, respectively. For instance, the differential and partial derivative of f with respect to a variable a are expressed as $\frac{df}{da}$ and $\frac{\partial f}{\partial a}$, respectively.

Sets can be represented by A , B , and C . For example, $A \subseteq B \cup C$ indicates that set A is a subset of the union of sets B and C . Random variables can be represented by X , Y , and Z . For example, the expectation of the sum of two random variables is given by $E(X + Y) = E(X) + E(Y)$. The symbol \mathbb{C} represents the set of complex numbers, such as $\exists z \in \mathbb{C} (z^2 + 1 = 0)$. \mathbb{Z}_n denotes the set of integers modulo n , and Z stands for the standard normal distribution. The symbol ω is used for the smallest infinite ordinal number, \aleph_0 represents the cardinality of natural numbers, and \mathfrak{c} denotes the cardinality of real numbers. Moreover, they are the key mathematical infinity symbols. The symbols \top and \perp represent tautology and contradiction, respectively. For example, for each proposition A , $A \wedge \top \equiv A$ and $A \wedge \neg A \equiv \perp$. These symbols are used in propositional logic, where \top denotes a statement that is always true, and \perp denotes a statement that is always false. In addition, $\sum_{i=m}^n a_i$ represents summation, $\prod_{i=m}^n a_i$ denotes the Pi product, and $[a]$ refers to the equivalence class of a . Δ refers to the discriminant, which is commonly used in polynomial equations to determine the nature of their roots. The symbols δ and ε represent small quantities used in proofs involving limits.

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