

# An Efficient Mechanism for Dynamic Survivable Multicast Traffic Grooming

Xiaojun Yu, Gaoxi Xiao\*, Tee Hiang Cheng

*School of Electric and Electronic Engineering, Nanyang Technological University,  
Singapore, 639798*

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## Abstract

Recent advances in wavelength division multiplexing (WDM) networks have helped enhance the popularity of multicasting services. However, as a single network failure may disrupt the information transmission to multiple end-users, protecting multicast requests against network failures becomes an important issue in network operation. This paper investigates the sub-wavelength level protection for dynamic multicast traffic grooming. A new method named Lightpath-Fragmentation based Segment Shared Protection (LF-SSP) scheme is proposed. By carefully splitting primary/backup light-paths into segments to improve resource sharing for both traffic grooming and protection, LF-SSP aims to minimize the network resources allocated for request protection. Extensive simulations are carried out to compare the performance of LF-SSP to some existing approaches, on sub-wavelength-level as well as wavelength-level multicast protections in different cases. Results show that LF-SSP steadily outperforms these existing methods as long as the network resources are not too limited. Influences of the add/drop port resources and the average number of destinations per connection request on the LF-SSP performance are also evaluated.

*Keywords:* Dynamic traffic grooming; Multicast; Lightpath fragmentation; Segment shared protection.

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\*Corresponding author

*Email addresses:* E070035@e.ntu.edu.sg (Xiaojun Yu), EGXXiao@ntu.edu.sg (Gaoxi Xiao), ETHCHENG@ntu.edu.sg (Tee Hiang Cheng)

## 1. Introduction

The increasing bandwidth demands over the past decades have driven wavelength-division-multiplexing (WDM) networks to become the dominant infrastructure for backbone networks [1]. In such networks, data is transmitted through all-optical wavelength channels, referred to as *lightpaths* [2], using optical-cross-connects (OXC). A lightpath may span several physical links. If all OXCs are not equipped with any wavelength converter, the lightpath has to be served using the same wavelength along its route, which is known as the *wavelength continuity constraint* [3].

Multicast involves the delivery of a message from a single source to a group of destinations simultaneously. As WDM networking technologies become mature, and bandwidth intensive multicast applications, such as interactive distant learning, high-definition-television (HDTV), live-video conferencing, etc., become increasingly popular, it is widely believed that a large portion of the future Internet traffic will be multicast in nature. To support the physical-layer multicasting, various methods utilizing either lightpath, or *light-tree* [4], or both have been proposed.

For many multicast sessions, the bandwidth they require is usually less than  $OC-3(155Mb/s)$ , which is much lower as compared to the capacity that can be provided by a single wavelength channel in today's WDM networks, e.g.,  $OC-192(10Gb/s)$ . To efficiently utilize wavelength capacity, *traffic grooming* [5] is usually adopted to pack multiple sub-wavelength granularity requests into a single wavelength channel for transmission. Multicast traffic grooming has received considerable attention, and the early-stage work has been mainly focusing on the static problems, wherein the network resources and all the traffic demands are known a priori [5–7]. In recent years, however, as more and more agile components are developed and widely deployed in optical networks, multicast traffic tends to show its dynamic nature and consequently, dynamic multicast traffic grooming is becoming increasingly important. With the requests arriving and leaving the networks dynamically, studies on dynamic multicast traffic grooming problem mainly focus on algorithm design for minimizing request blocking probability or maximizing network throughput, e.g., [7–9].

Optical networks are vulnerable to various component failures, and a single failure may cause massive information losses and serious service interruptions. In networks supporting a large number of bandwidth-intensive multicast applications, influences of network failures could be even more

devastating. Having proper survivability mechanisms to protect multicast sessions against network failures is therefore of essential importance. Generally speaking, the network survivability methods can be classified into two categories: *restoration* [10] and *protection* [11]. While restoration is reactive with efficient resource utilization, protection is proactive and recovers more quickly after the failures. In high-speed WDM backbone networks, protection is usually regarded as a more favorable option as it guarantees full recovery and faster restoration speed [12].

A number of multicast protection mechanisms have been proposed in literature [13–19]. According to whether backup resources can be shared or not, such protection mechanisms can be classified into *dedicated* or *shared* protections; while according to how the backup route is calculated, they can be classified into five categories [17]: *tree*-based, *ring*-based, *path*-based, *segment*-based, and *cycle*-based. Results in [18, 19] showed that the tree- and ring-based methods are not resource efficient, while the cycle-based ones are not flexible enough for dynamic request protection, especially for the dynamic multicast requests. Between the path-based and segmented-based schemes, the latter one is reported to achieve better blocking performance, faster restoration speed and higher resource efficiency in protecting wavelength-level multicast requests [19].

Compared to the extensive research efforts dedicated towards wavelength-level multicast request protection, sub-wavelength-level multicast request protection, which is also known as survivable multicast traffic grooming (SMTG), has received rather limited attention: though two methods, which will be reviewed in Section 2.3, have been proposed in [20] for SMTG, some assumptions adopted therein may not necessarily be valid in modern optical communication networks. Specifically, as pointed out in [18], in current backbone networks, the capacity reserved for protection within a fiber cannot be utilized in two opposite directions by simply reconfiguring the switches at its two end nodes. Therefore, we do not adopt such assumptions in our proposed scheme.

In this paper, we address the problem of protecting sub-wavelength-level multicast requests in dynamic traffic grooming process. A novel mechanism, named lightpath-fragmentation based segment shared protection (LF-SSP) scheme, is proposed to protect multicast requests at the connection level. The primary objective of the algorithm design is to protect requests against any single link failure while minimizing the network’s bandwidth blocking

ratio (BBR), which is defined as

$$BBR = \frac{\sum \text{Blocked request bandwidth}}{\sum \text{Bandwidth of all requests}}$$

By adopting the lightpath fragmentation (LF) method to fragment new lightpaths into shorter segments to improve resource sharing for both traffic grooming and request protection, the LF-SSP scheme attempts to minimize the network resources allocated to protect each request. To evaluate the performance of LF-SSP, extensive simulations are carried out. We firstly compare the LF-SSP scheme against an existing method for sub-wavelength-level multicast request protection, and then extend the comparison to a few existing methods for wavelength-level request protection. Simulation results demonstrate that LF-SSP outperforms the existing methods in different cases as long as the network resources are not too limited. In addition, the effects of a few factors, including the redundancy level of add/drop port resources and the average number of destinations per multicast session, are also evaluated.

The remainder of this paper is organized as follows. Section 2 defines the network model and the problem to be addressed, followed by a brief description of related work. Section 3 describes the proposed LF-SSP scheme for dynamic SMTG. The simulation results are presented and discussed in Section 4. Section 5 concludes the paper.

## 2. Network Model and Problem Definition

### 2.1. Network Model

We consider dynamic multicast traffic grooming problem in wavelength-routed WDM networks. The network is represented by a directed graph  $G = (V, E)$ , where  $V$  and  $E$  denote the sets of network nodes and fiber links, respectively. Specifically, we assume that the physical-layer topology of the network is a set of nodes interconnected by fiber links. Each fiber link is composed of two fibers in opposite directions, each of which carrying  $W$  wavelengths. The capacity of each wavelength is  $B$  units. Each network node is equipped with a grooming-capable optical cross-connect (GC-OXC) [7] as shown in Fig. 1. Each GC-OXC is equipped with a certain number of add/drop ports, which generally equals the number of transceiver pairs on the node. As both the add/drop ports and the transmitters/receivers are

107 high-cost components, a network node is usually equipped with a limited  
 108 number of ports shared by all wavelengths going through it. In this paper,  
 109 we define the *add/drop ratio*  $r$  ( $0 < r \leq 1$ ) as the ratio of the number of  
 110 add/drop port pairs over the total number of wavelengths passing-through  
 111 the OXC. We refer to a network node with  $r < 1$  as a port-limited node; and  
 112 a port-unlimited one otherwise.

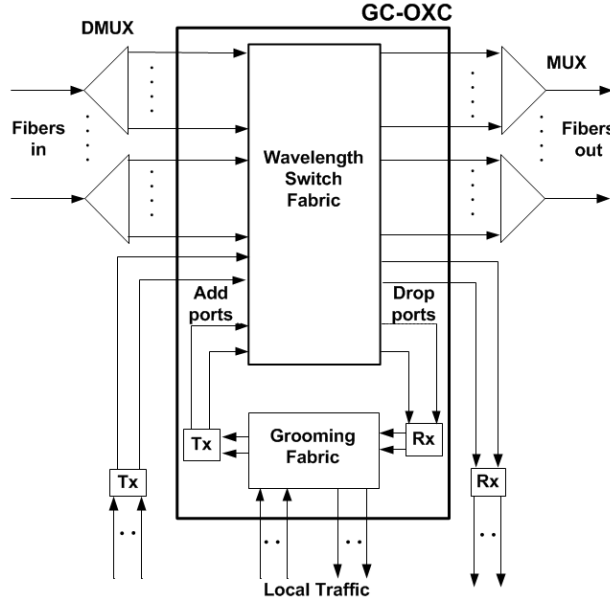


Figure 1: A typical grooming-capable OXC architecture.

113 To support multicasting services, a lightpath-based scheme is adopted in  
 114 this paper: as demonstrated in our previous study [9], the lightpath-based  
 115 approaches steadily outperform the light-tree based ones in achieving better  
 116 bandwidth blocking performance for dynamic multicast traffic grooming. A  
 117 lightpath occupies a wavelength along its route, a transmitter at its source  
 118 node, and a receiver at its destination node, whereas a multicast request  
 119 may traverse several lightpaths along its route, and consumes a portion of  
 120 the bandwidth provided by each lightpath it traverses.

## 121 2.2. Problem Statement

122 The dynamic SMTG problem in WDM networks can be formulated as  
 123 follows. Upon the arrival of each multicast request  $R\{s, D, b\}$ , where  $s$ ,  
 124  $D$  and  $b$  denote the request source, specified destination set and required

bandwidth respectively, the central network controller must identify both primary and backup routes for the request using accurate global information regarding the network state, so that the request can survive any single link failure. The primary objective of the algorithm design is to minimize the network BBR by improving resource sharing in both the traffic-grooming and request-protection processes.

We assume that all multicast requests arrive/leave the network dynamically with no prior information regarding future requests, and that a request is supported only when all its destinations can be served; otherwise the request will be blocked. All requests are protected at the connection level, i.e., the connection to each request destination shall pass through a certain number of *survivable* lightpaths. A lightpath is “survivable” if it is protected by a link-disjoint backup path, which may pass through one or multiple lightpaths with sufficient bandwidth reserved for backup purpose. The backup paths of different survivable lightpaths can share capacities if their primary paths are link-disjoint. Since it is shown in [21] that grooming primary and backup paths separately helps improve the network blocking performance, we adopt the same grooming mechanism in this paper. We refer to lightpaths that are utilized for working paths as *working lightpaths*, and those solely for request protection as *backup lightpaths*.

To be more precise, in this paper, we assume that each fiber link comprises two directional fibers in opposite directions and that a single link failure will sever the fibers in both directions. We also assume that an ongoing transmission cannot be interrupted until it is completed.

### 2.3. Related Existing Work

The problem of wavelength-level multicast request protection has been extensively studied, and various link-, path- and segment-based protection schemes have been proposed [13–19]. Among them, the segment-based protection schemes, as discussed in Section 1, are believed to achieve the best blocking performance for dynamic multicast request protection; hence, a segment-based protection scheme is considered in this paper.

The first segment-based protection method was proposed in [13]. By protecting each segment on the primary tree using a link-disjoint path from the segment source to its end node, the proposed segment-based method is able to protect a multicast session against any single link failure. By adopting a similar idea, a different segment-based mechanism known as the Segment-based Protection Tree (SPT) was proposed in [18]. With the SPT

162 scheme, each primary tree is divided into tree-segments, each of which is  
 163 then protected by a link-disjoint tree that connects the session source and  
 164 all its destinations. The minimum-cost survivable topology, which takes into  
 165 account the costs for both the primary and backup trees, is chosen to fulfill  
 166 the connection request. It has been demonstrated that the SPT mechanism  
 167 outperforms the best existing path-based method in certain cases.

168 More recently, another new segment-based protection method known as  
 169 level-protection (LP) was proposed in [19]. Once a primary tree has been  
 170 found, the LP scheme attempts to protect the session destinations one by  
 171 one in an ascending order of their distances from the request source, with  
 172 the objective of efficiently sharing resources on both the primary and backup  
 173 trees. The LP scheme has been demonstrated to achieve superior perfor-  
 174 mance with respect to the algorithms proposed in [14, 16].

175 To date, the problem of sub-wavelength-level dynamic SMTG has received  
 176 limited attention. The authors of [20] have proposed the first two algorithms,  
 177 namely Multicast Traffic Grooming with Segment Protection (MTG-SP) and  
 178 Multicast Traffic Grooming with Shared Segment Protection (MTG-SSP)  
 179 respectively, attempting to address this problem. As discussed in Section 1,  
 180 however, as the assumptions adopted by these algorithms are not necessarily  
 181 valid in modern optical network infrastructures, while the implementations  
 182 of these methods strongly rely on these assumptions, we would not include  
 183 these two methods for comparison in this paper.

184 In [22], we proposed a scheme known as connection-level segment shared  
 185 protection (CL-SSP) scheme for SMTG. For each multicast request, CL-SSP  
 186 attempts to protect it against any single link failure at the connection level.  
 187 To improve resource sharing, CL-SSP adopts a simple method to fragment  
 188 the new primary/backup lightpaths into shorter segments on those interme-  
 189 diate nodes with redundant transceiver resources. Our results indicated that  
 190 such a simple approach, although very effective in fulfilling the multicast  
 191 transmissions without protection [9], may not easily achieve satisfactory per-  
 192 formance for dynamic SMTG. Among the several methods we investigated,  
 193 the best performance was achieved by fragmenting only the backup paths.  
 194 To further improve the network performances, better approaches for more  
 195 effective lightpath fragmentation are needed.

196 In this paper, we propose a new LF-SSP method in which both working  
 197 and backup lightpaths are carefully fragmented with the objective of mini-  
 198 mizing network BBR. The BBR performance of the new method is compared  
 199 against those of the best existing wavelength-level schemes including the SP-

200 T and LP methods, and that of the sub-wavelength level CL-SSP method in  
 201 which only the backup lightpaths are fragmented. For simplicity, we hence-  
 202 forth refer to CL-SSP scheme with only backup path fragmentation simply  
 203 as the CL-SSP method.

### 204 3. LF-SSP Mechanism for Survivable Dynamic Multicast Traffic 205 Grooming

206 This section presents the proposed LF-SSP mechanism in detail. We first  
 207 briefly describe the main idea of the segment shared protection (SSP) method  
 208 for dynamic SMTG and then discuss the major steps of the proposed two-  
 209 phase LF-SSP method. Finally, the detailed LF-SSP mechanism is presented.

#### 210 3.1. Segment Shared Protection (SSP) Method

211 Segment shared protection is an efficient mechanism that has been uti-  
 212 lized to support survivable unicast [21, 23, 24] and multicast transmissions  
 213 [13, 18, 19]. For unicast services, the basic concept of SSP is to split the work-  
 214 ing path into a few segments and then protect each of them separately. It has  
 215 been demonstrated in the literature that properly designed segment protec-  
 216 tion can achieve better blocking performance than path- or link-protection  
 217 methods [21, 23, 24]. The example presented in Fig. 2 illustrates the higher  
 218 resource sharing efficiency of the SSP scheme: when a path-protection scheme  
 219 is adopted, as shown in Fig. 2(a), the backup-path capacity along the light-  
 220 path from s to d cannot be shared when serving the new request from s' to  
 221 d', whereas when a segment-protection scheme is adopted, capacity sharing  
 222 of the backup lightpaths is permitted, as shown in Fig. 2(b).

223 To support survivable multicast requests, SSP attempts to fragment a  
 224 multicast tree into segments, e.g., a number of paths or smaller trees, and  
 225 then protect each segment separately using a link-disjoint path. Meanwhile,  
 226 to improve resource utilizations, the backup resources for different segments  
 227 can be shared. Typically, there are two approaches for backup resource  
 228 sharing: *self-sharing* and *cross-sharing* [25]. Self-sharing refers to the sharing  
 229 of resources among backup routes within the same session, and cross-sharing  
 230 refers to the sharing of backup resources among different sessions.

231 In this paper, both self- and cross-sharing are considered in the proposed  
 232 SSP scheme. Specifically, to identify the sharing potential of the backup  
 233 paths, each backup lightpath is associated with a link set  $A$ . Consider a  
 234 backup lightpath  $e$ : its associated link set can be described as  $A = \{a | a \in$



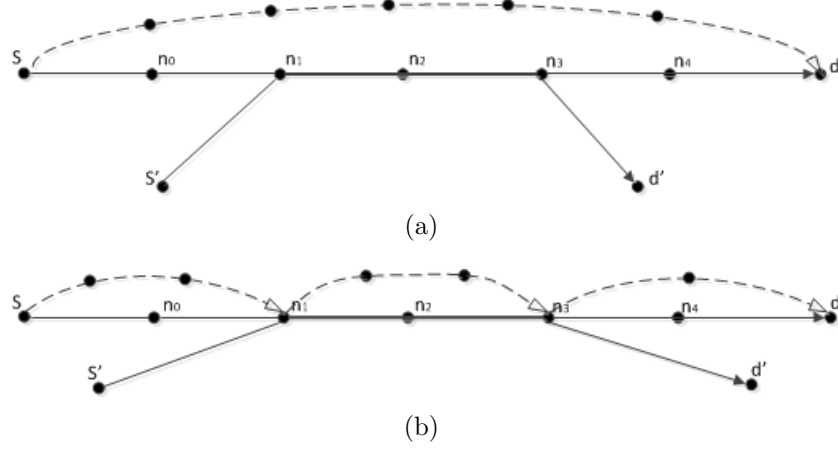


Figure 2: A comparison between the shared path protection and SSP against single link failure: (a) shared path protection; (b) SSP.

$E, 0 < b_e^a \leq B\}$ , where  $b_e^a$  represents the amount of capacity that would be rerouted to  $e$  if its protected link  $a$  fails. Hence, the total amount of capacity that has been reserved for protection on  $e$  is  $b_t = \max_{a \in A} b_e^a$ , and its residual capacity is  $r_m = B - b_t$ . The capacity along  $e$  that can be shared by the backup path of any new primary lightpath  $l$ , which is link-disjoint to  $e$ , is  $b_f^l(L) = b_t - \max_{a \in (L \cap A)} b_e^a$ , where  $L$  denotes the set of physical links that  $l$  goes through. Note that  $b_f^l(L)$  is non-negative.

The proposed SSP mechanism consists of two phases: the first phase is to establish a primary tree routing from the request source to all its destinations using the existing survivable lightpaths as much as possible, and setting up new primary lightpaths only when such is necessary; the second phase is to protect each new primary lightpath, if any, against any single link failure using SSP scheme. As we have previously demonstrated in [22], properly fragmenting new primary/backup lightpaths into shorter ones helps improve network BBR performance, a lightpath-fragmentation (LF) method is adopted in the proposed SSP method to conservatively split new lightpaths into shorter ones. In this manner, the SSP scheme attempts to minimize the total amount of network resources allocated for routing and protecting each request

Below we present the detailed two-phase SSP scheme for dynamic SMTG.

### 255 3.2. Two-Phase SSP Scheme for Dynamic SMTG

#### 256 (i) First-phase Primary Tree Route Calculation

257 As aforementioned, since establishing new lightpaths consumes addition-  
 258 al wavelength and transceiver resources, we use the existing survivable light-  
 259 paths to serve as many request destinations as possible, and new lightpaths  
 260 are established to serve the remaining destinations only when such is neces-  
 261 sary.

262 It is well known that identifying the minimal-cost primary tree route is an  
 263 NP-complete problem. We adopt the simple yet efficient minimum cost path  
 264 heuristic (MPH) [26] to connect the request destinations one by one to the  
 265 primary tree. Procedure I presents the process for calculating the primary  
 266 route  $T$  for a multicast request.

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#### **Procedure I:** Primary\_Route\_Calculation\_sub\_Algorithm

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**input** : A network  $G(V, E)$  and a multicast request  $R\{s, D, b\}$ .  
**output**: A primary tree route  $T$  for serving  $R\{s, D, b\}$ .  
 1 Generate an auxiliary graph (AG) using all the existing survivable lightpaths; Call  
**MPH** on AG to initiate a tree from  $s$  to as many members of  $D$  as possible.  
 Remove those served members from  $D$ . If  $D$  is empty, go to Step 12; otherwise, save  
 the partial tree  $T$ , and continue. // *Grooming with existing survivable lightpaths*  
 2 Add  $s$  and all the other nodes on  $T$  to a node set  $S$ ; // *optical layer primary tree*  
*routing (2-11)*  
 3 **while**  $D \neq \Phi$  **do**  
 4     Generate an optical-layer AG; calculate all-to-all shortest paths between each  
    node in  $S$  to each node in  $D$  by adopting a certain lightpath cost definition;  
 5     Choose the shortest path among all paths that connecting any member of  $S$  to  
    any member of  $D$ . If there is a tie, break it randomly. Denote the selected path  
    as  $P$ , the end node of  $P$  in  $D$  as  $d$ , and the length of  $P$  as  $dis$ .  
 6     **if**  $dis < \infty$  **then**  
 7          $S = S \cup \{d\}$ ;  $D = D \setminus d$ ; save the path  $P$  onto the primary tree  $T$ ;  
 8     **else**  
 9         Block the request  $R\{s, D, b\}$  and break;  
 10    **end**  
 11 **end**  
 12 Return the primary tree route  $T$ .

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267 Step 1 attempts to utilize the existing survivable lightpaths to serve as  
 268 many request destinations as possible. If there are sufficient existing surviv-  
 269 able lightpaths, the request will be served directly; otherwise, the remaining  
 270 destinations will be connected to the primary tree one by one using new  
 271 lightpaths as shown in Steps 2 – 11.

272 Note that various path cost definitions can be adopted in Step 4 to define  
 273 the distance between two nodes. To improve the network's BBR performance  
 274 while balancing the resource consumptions, the cost definition shown below  
 275 is adopted [9],

$$C_{ij} = \begin{cases} \frac{1-r}{p \times r \times (\bar{H}+1)} - H_{ij} \ln \left(1 - \frac{1}{\omega_{ij}+1}\right) & \text{if } \omega_{ij} > 0 \text{ and } p > 0 \\ \infty & \text{if } \omega_{ij} = 0 \text{ or } p = 0 \end{cases} \quad (1)$$

276 where  $p$  is the smaller one among the number of transmitters on the source  
 277 node and the number of receivers on the destination node of the lightpath,  
 278  $\omega_{ij}$  is the number of wavelengths available along the lightpath route,  $\bar{H}$  is  
 279 the average path length of the network, and  $H_{ij}$  is the minimum hop length  
 280 between the two end-nodes of the lightpath. The intent of this function is to  
 281 balance the consumptions of wavelength and transceiver resources. Specif-  
 282 ically, if both resources are abundant, the costs of consuming them will be  
 283 low and not so different from each other; whereas if either becomes scarce,  
 284 the cost of consuming the scarce resource will be increased. Our previous  
 285 studies demonstrated that such a definition steadily leads to satisfactory per-  
 286 formance [9].

#### 287 (ii) Second-Phase LF-Based SSP

288 Once the primary tree route is identified for a request in the first phase,  
 289 the proposed method enters its second phase to identify a backup route  
 290 for each new primary lightpath, wherein auxiliary graphs are generated for  
 291 routing purpose.

##### 292 3.2.1. Graph Generation for Backup-Route Calculation

293 For each new lightpath added into the primary tree route  $T$ , the SSP  
 294 scheme is adopted to protect it at the connection level. Specifically, a new  
 295 lightpath is usually fragmented into segments, which we refer to as *active*  
 296 *segments* (ASs) following [23], and each segment is protected using one or  
 297 more link-disjoint *backup segments* (BSs). For example, the new primary  
 298 lightpath shown in Fig. 2(b) is fragmented into three ASs, i.e.,  $S \rightarrow n_1$ ,  
 299  $n_1 \rightarrow n_3$ , and  $n_3 \rightarrow d$ , and each AS is protected by a separate link-disjoint  
 300 BS. The nodes  $n_1$  and  $n_3$ , each of which acting as the source node of a  
 301 segment, are called *switching nodes*.

302 To identify backup routes for a multicast session  $R\{s, D, b\}$ , a complete  
 303 auxiliary graph with appropriate edge costs is generated. In such a graph, an  
 304 edge represents either an existing backup lightpath that has been established

305 or a new lightpath to be established between two network nodes. Suppose  
 306 that  $P$  is a new primary lightpath to be protected, AS is an active segment  
 307 of  $P$ , and SG is the set of links that AS traverses. The link-cost assignment  
 308 policy below is adopted for the calculation of AS's backup route:

$$L_{ij} = \begin{cases} \infty & \text{a backup lightpath } e \text{ that is link-disjoint to AS cannot} \\ & \text{be found between node } i \text{ and } j; \\ \varepsilon + b_{ad} & \text{an existing backup lightpath } e \text{ that is link-disjoint to} \\ & \text{AS has a capacity } r_m + b_f^{AS}(SG) > b; \\ b \times C(e) & \text{a new backup lightpath that is link-disjoint to AS} \\ & \text{needs to be set up.} \end{cases} \quad (2)$$

309 where  $\varepsilon$  is a small positive value ( $10^{-2}$  used in the paper) and  $b_{ad}$  is  
 310 the amount of additional capacity that should be reserved on the exist-  
 311 ing backup lightpath for AS protection. It can be calculated as  $b_{ad} =$   
 312  $\max(0, b - b_f^{AS}(SG))$ .

313 As indicated in Eq. (2), for those existing backup lightpaths that have  
 314 enough residual capacities, their costs approximately equal the additional  
 315 capacity that has to be reserved for the request protection; while for new  
 316 backup lightpaths to be established, their costs equal the request bandwidth  
 317 times parameter  $C(e)$ , which is defined as follows:

$$C(e) = \begin{cases} \left( \frac{(1-r)}{p \times r(H+1)} - H_e \ln \left( 1 - \frac{1}{\omega_e + 1} \right) \right) \times amp & \text{if } \omega_e > 0 \text{ and } p > \\ 0 & \\ \infty & \text{if } \omega_e = 0 \text{ or } p = 0 \end{cases} \quad (3)$$

318 where all symbols have the same meanings as those defined in Eq. (1), and  
 319  $amp$  is an amplification factor. This definition ensures that the typical cost  
 320 for establishing a new backup lightpath, i.e.,  $C(e)$ , is approximately 5 times  
 321 as much as that of using an existing lightpath (The cost of using an existing  
 322 lightpath is 1 by default.) when the network is in its typical operation status  
 323 [28]. (In this paper, we assume that  $\omega_e = W/2$  for the typical network status.  
 324 A detailed discussion on this assumption may refer to [27].).

325 Once the auxiliary graph is generated, any shortest-path algorithm can  
 326 be applied to identify a backup route for each primary path. However, since  
 327 long lightpaths may impose a strict wavelength continuity constraint on the  
 328 lightpath routing, thereby degrading resource sharing in the grooming pro-  
 329 cess, an LF method is adopted in the proposed SSP mechanism for both AS  
 330 determination and BS fragmentation.

331 Below, we briefly review the LF method proposed in [22], pointing out its  
 332 limitation in network protection scenarios, and finally propose an improved  
 333 LF-based method for SMTG.

### 3.2.2. Greedy LF Method for AS Determination and BS Fragmentation [22]

Suppose that  $L$  is a primary/backup route along which a new wavelength should be reserved;  $n$  is an intermediate node of  $L$  with a fan-out degree of  $d_n$ . The numbers of free transmitters and receivers on  $n$  are denoted by  $T_n$  and  $R_n$  respectively, and the numbers of free wavelengths along the incoming and outgoing links of  $n$  are denoted by  $\omega_{in}$  and  $\omega_{out}$  respectively. The three parameters defined as below are used to determine whether the path  $L$  should be segmented at  $n$ :

$$\alpha_m = \min\left(\frac{T_n}{d_n \times \omega_{out}}, \frac{R_n}{d_n \times \omega_{in}}\right), \quad (4)$$

$$\alpha_n^p = \frac{1}{H_n^p}, \quad (5)$$

$$\alpha_n^b = \frac{1}{H_n^b}, \quad (6)$$

where  $H_n^p$  and  $H_n^b$  are two topology-dependent constants denoting the average shortest primary and backup path lengths from  $n$  to all other network nodes, respectively. Specifically, with a given network topology,  $H_n^p$  is averaged over all the shortest primary lightpaths from  $n$  to each of the other network nodes, and  $H_n^b$  is averaged over all the corresponding shortest backup lightpaths.

In the above equations,  $\alpha_m$  denotes the smaller one of the add and drop ratios on node  $n$  for the current network status;  $\alpha_n^p$  and  $\alpha_n^b$  are inversely proportional to the average primary and backup lightpath lengths from  $n$  to all the other network nodes respectively. The comparison between  $\alpha_m$  and  $\alpha_n^p$  or  $\alpha_n^b$  helps indicate the relative availability of the port resources at node  $n$  for lightpath fragmentation under the current network status. When  $\alpha_m > \alpha_n^p$  in a primary lightpath ( $\alpha_m > \alpha_n^b$  in a backup lightpath), it indicates that the transceiver resources at  $n$  are relatively redundant and it may be beneficial to segment  $L$  at  $n$  to avoid establishing too long lightpaths, and thereby alleviates the wavelength continuity constraint on  $L$ 's establishment; otherwise, the transceiver resources are regarded as relatively limited on node  $n$ , and it is better for  $L$  to bypass  $n$  to conserve transceiver resources.

We refer to a node  $n$  as a *fragment node* if  $\alpha_m > \alpha_n^p$  for a primary lightpath or  $\alpha_m > \alpha_n^b$  for a backup path that passes through  $n$ . Procedure II presents the major steps of the LF method.

A naive approach to apply the LF method is to adopt a greedy approach which segments a lightpath on a node whenever the transceiver resources

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**Procedure II:** Lightpath\_fragmentation\_scheme(LF)

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**input** : A network  $G(V, E)$ , a lightpath  $L$   
**output**: A set of new lightpaths.

```
1 while (any node of  $L$  has not been checked) do
2   for each intermediate node (if any)  $n$  along  $L$  do
3     Calculate  $\alpha_m$  for  $n$  ;
4     if  $\alpha_m > \alpha_n^p$  for the primary path (or  $\alpha_m > \alpha_n^b$  for the backup path) going
       through  $n$  then
5       Fragment  $L$  at  $n$ , and obtain two new lightpaths  $L_a$  and  $L_b$ ;
6        $L = L_b$ ;
7     end
8   end
9 end
```

---

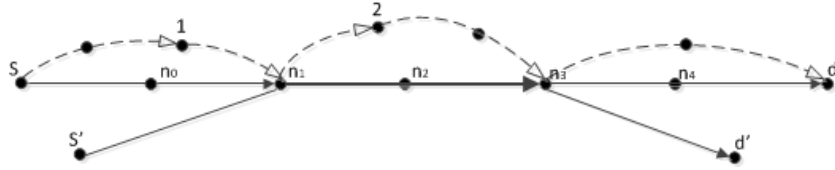


Figure 3: LF method adopted for primary path protection.

on this node are relatively redundant. An example is illustrated in Fig. 3, where a survivable lightpath is fragmented on nodes  $n_1$ ,  $n_3$ , 1, and 2. Though such an approach helps alleviate the wavelength continuity constraint and achieve satisfactory performance in optical networks without protection, our previous results demonstrated that it may actually degrade the network BBR performance in SMTG [22]: protecting a large number of ASs requires a large amount of protection resources.

Inspired by such observation, we propose to apply the LF method conservatively for lightpath protection within the proposed SSP scheme. Specifically, we develop a lightpath segmentation process similar to that applied in the PROMISE method in [23], with the objective of minimizing the network resources allocated for protecting each request.

### 3.2.3. Improved LF method for dynamic SMTG

After the first-phase route provisioning, we have obtained a primary tree that may contain some new primary lightpaths. The task now is to find the best fragmentation of these new primary lightpaths so that the resources

380 allocated for protecting them are minimized. Denote a new lightpath as  $P$ ,  
381 the number of optical hops that  $P$  traverses as  $h$ , and label the nodes along  
382  $P$  from 0 to  $h$ . Assume that  $m$  ( $0 < m < h$ ) is an intermediate node on  
383  $P$ ,  $AS_m$  is a candidate active segment from node  $m$  to node  $h$  along  $P$ ,  $C_m$   
384 is the shortest link-disjoint backup path that can protect  $AS_m$ , and  $C_{m,i}$  is  
385 the shortest backup path that has been identified for protecting the active  
386 segment between node  $m$  and node  $i$  ( $i < m < h$ ). Denote the costs of the  
387 latter two paths as  $C(m)$  and  $C(m,i)$ , respectively. Note that they are the  
388 sums of the costs of all backup lightpaths that  $C_m$  and  $C_{m,i}$  have traversed  
389 respectively. By adopting a similar main idea as that of the PROMISE  
390 method, Procedure III presents the major steps of the improved LF-method  
391 for backup-route calculation.

392 Procedure III begins by testing each node along the primary lightpath  
393  $P$ , in a backward direction starting from the node adjacent to the end node  
394  $h$ , to find all the candidate segment points where  $\alpha_m > \alpha_m^p$  in Step 3. For  
395 each identified candidate fragment node (denoted as  $m$ ), the corresponding  
396 minimum-cost link-disjoint backup path between nodes  $m$  and  $h$  is calculat-  
397 ed in Steps 4-6. Steps 7-13 recursively test all the candidate fragment nodes  
398 between  $m$  and  $h$ , if any, with the objective of finding the minimum-cost  
399 segment protection path between  $m$  and  $h$ . Finally, when the testing on the  
400 primary lightpath nodes reaches the starting node 0, the minimum-cost seg-  
401 ment protection path for the new primary lightpath is found. Note that the  
402 backup route BS may contain both existing backup lightpaths and new ones  
403 to be established. We adopt a simple policy that a new backup lightpath  
404 is segmented on all the candidate fragment nodes where  $\alpha_m > \alpha_n^b$ . Our  
405 simulation results show that such a simple approach steadily leads to sat-  
406 isfactory performance. In other words, good performance is achieved when  
407 we adopt conservative segmentation on the primary lightpaths yet greedy  
408 segmentation on the backup lightpaths.

409 It is easy to see that for a new lightpath with  $h$  candidate segment nodes,  
410 the number of BSs that we need to calculate is limited to  $h(h+1)/2$ . Here we  
411 count the starting node of the lightpath also as a candidate segment node.

412 Finally, we compare the complexity of LF-SSP to those of the existing  
413 wavelength- and subwavelength-level methods. For an arriving request with  
414 destination size  $D$ , all these methods firstly find a minimum spanning primary  
415 tree (MST) with a complexity of  $O(D|V|^2)$ , where  $|V|$  is the number of  
416 network nodes. SPT method then protects each segment of such MST using  
417 a link-disjoint tree, its complexity hence is  $O(D|V|^3)$ ; LP protects the request

---

**Procedure III: LF-based Backup Path Provisioning**


---

**input** : A network  $G(V, E)$ , and new primary lightpath  $P$  for  $R\{s, D, b\}$ .  
**output**: A set of backup lightpaths to protect  $P$ .

- 1 Clear the fragment node set  $S_F$ ;
- 2 **for** each intermediate node  $m = h - 1$  to 0 along  $P$  **do**
- 3     **if**  $m$  is fragment node with  $\alpha_m > \alpha_m^p$  **then**
- 4         Set the links from  $m$  to  $h$  along  $P$  to be  $AS_m$  ;
- 5         Generate an auxiliary graph (AG) for backup path routing according to Eq. (2); *// Graph generation for backup routing*
- 6         Calculate the shortest path that is link-disjoint to  $AS_m$  on AG for its protection; denote its cost as  $C(m)$ , and record such path as  $C_m$ ; *//  $C_m$  initialization*
- 7         **for** each node  $i$  in  $S_F$  **do**
- 8             Set AS to be the links from  $m$  to  $i$  along  $P$  ;
- 9             Generate another new auxiliary graph (AG') according to Eq. (2); *// graph generation for AS protection*
- 10            Calculate the shortest path that is link-disjoint to AS from  $m$  to  $i$  on AG' to protect AS, and denote this path by BS; *// backup routing*
- 11            Call Procedure II (Lightpath Fragment scheme) to process each new backup lightpath along BS and return a set of new lightpaths, calculate the cost  $C(m, i)$  using Eq. (2); record the processed BS route as  $C_{m,i}$ ; *// LF for backup route processing;*
- 12            Choose the backup route with smaller cost for  $AS_m$  protection:  
 $C_m = \min(C_m, C_{m,i} + C_i)$ ; *// choose the back route for  $AS_m$*
- 13         **end**
- 14          $S_F = S_F \cup \{m\}$
- 15     **end**
- 16 **end**
- 17 Return  $C_0$  for protecting the new lightpath  $P$ .

---



destinations on the MST one by one in an ascending order of their distances from the source, with a complexity of  $O(D^2|V|^2)$ . CL-SSP protects each new lightpath on the MST using a link-disjoint path its complexity therefore is  $O(D|V|^2 + D(|E| + |V|\log(|V|)))$  with  $|E|$  being the number of network links. For the LF-SSP method, since it adopts Procedure III to minimize the resources for both request grooming and protection, its complexity is  $O(D|V|^2) + D^2(|E| + |V|\log(|V|))$  in the worst case. In a backbone network with a moderate number of network nodes, the complexity of LF-SSP is acceptable.

Using the primary- and backup-route provisioning sub-algorithms described above, we now present the proposed LF-SSP mechanism for SMTG.

### 3.3. The Proposed LF-SSP Mechanism

Algorithm I presents the major steps of the proposed LF-SSP mechanism.

To encourage traffic grooming when fulfilling a request, LF-SSP gives higher priority to the use of existing survivable lightpaths. Hence, Step 1 attempts to identify a primary route  $T_P$  for the request, and if a tree route that comprises only existing survivable lightpaths exists, it will be adopted to directly fulfill the request; otherwise, new lightpaths must be established for the request. Steps 2 – 5 attempts to protect each new primary lightpath on  $T_P$  using the LF-based backup-path calculation sub-algorithm to minimize the amount of backup resources allocated for each lightpath; if a backup route cannot be found for any primary lightpath, the request will be rejected. Steps 6 – 20 allocate the required network resources for a survivable lightpath, and finally Step 21 updates the network status. Note that for both the traffic grooming in Step 1 and the lightpath wavelength assignment in Steps 6 – 20, the first-fit wavelength-assignment policy is adopted if there is more than one candidate route.

## 4. Performance Evaluation

In this section, we conduct a number of simulations to evaluate the performance of the LF-SSP mechanism in different cases. We first present the simulation setup and then compare LF-SSP method against a few existing approaches for sub-wavelength- and wavelength-level multicast request protection; finally, we assess the influences of a few factors on LF-SSP performance.

---

**Algorithm I:** LF-SSP for dynamic multicast traffic grooming

---

**input** : A network  $G(V, E)$  and a multicast request  $R\{s, D, b\}$ .  
**output:** A survivable multicast tree route for  $R\{s, D, b\}$ .

- 1 Call Primary\_Route\_Calculation\_sub\_Algorithm, which returns a primary route  $T_P$ ;  
if  $T_P$  consists only of existing survivable lightpaths, go to Step 21 and otherwise,  
continue;
- 2 **for** each new lightpath  $P$  on  $T_P$  **do**
- 3     Call LF\_based\_Backup\_Path\_Provisioning for  $P$  protection;
- 4     If backup paths (BSs) can be found for  $P$ , assign the BSs to  $P$  and denote  $P$   
as survivable on  $T_P$ ; otherwise, block the request;
- 5 **end**
- 6 **for** each new primary lightpath  $P$  on  $T_P$  **do**
- 7     Fragment  $P$  according to its BSs; allocate transceiver and wavelength  
resources to each fragmented new AS of  $P$ ; if any resource is unavailable, block  
the request;
- 8     **for** each new backup lightpath along the BSs **do**
- 9         Call Procedure II to fragment the lightpath, if possible;
- 10        **for** each new lightpath  $L$  obtained from fragmentation **do**
- 11          Reserve a wavelength along its route;
- 12          **if** source node of  $L$  is neither  $s$  nor a fragment node on  $P$  **then**
- 13             Allocate a transmitter at this node;
- 14          **end**
- 15          **if** end node of  $L$  does not belong to  $D$  or is not a fragment node on  $P$   
**then**
- 16             Allocate a receiver at this end node;
- 17          **end**
- 18        **end**
- 19     **end**
- 20 **end**
- 21 Update the residual capacities of all survivable lightpaths along route  $T_P$ .

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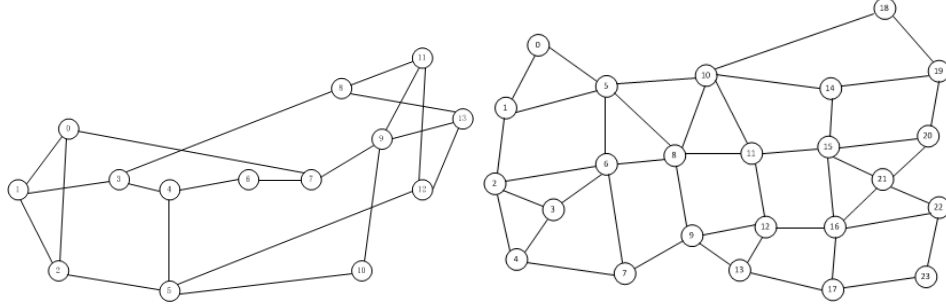


Figure 4: Two network topologies utilized for simulations. (a) 14-node 21-link NSFnet topology and, (b) 24-node 43-link USnet topology.

#### 4.1. Simulation Setup

We simulate a dynamic network environment to evaluate LF-SSP performance in different cases. We assume that all requests arrive/leave the network dynamically according to a Poisson distribution with mean rate  $\lambda$  and that their holding time is negative exponentially distributed with a mean  $\mu = 1$ ; the request source and destinations are randomly chosen among all network nodes, and the number of destinations of each request, denoted by  $N$ , follows a truncated geometric distribution [8] with a parameter  $q$  ( $0 < q < 1$ ). Specifically, the probability that a request has  $k$  destinations, and the mean number of the request destinations are given by Eq. (7) and Eq. (8), respectively,

$$P(N = k) = \frac{(1 - q)q^{k-1}}{q - q^{|V|}}, 2 \leq k \leq |V| - 1 \quad (7)$$

$$\begin{aligned} E(N) &= \sum_{k=2}^{|V|-1} k \times P(N = k) \\ &= \frac{2q - q^2 - |V|q^{|V|-1} + (|V| - 1)q^{|V|}}{(1 - q)(q - q^{|V|-1})} \end{aligned} \quad (8)$$

where  $|V|$  is the number of network nodes.

Two commonly used network topologies as shown in Fig. 4 are utilized for simulation, which are 14-node, 21-link NSFnet and 24-node, 43-link USnet. We assume that

- 467 1. Each network link consists of two fibers travelling in opposite directions,  
468 each carrying  $W = 32$  wavelengths; the full capacity of each wavelength  
469 is  $B = 16$  units; *amp* is set to be 40 and 25 for NSFnet and USnet,  
470 respectively;
- 471 2. The average number of destinations of each session is 3. For sub-  
472 wavelength requests, the required bandwidth is an integer uniformly  
473 distributed in the interval  $[1, 16]$ , whereas for wavelength-level multicast  
474 requests, their required bandwidth is 16 units.
- 475 3. The number of transceivers on a network node is  $W \times d_i \times r$ , where  $d_i$   
476 is the fan-out degree of the node;
- 477 4. Loss of signal power due to transmission attenuation or light-splitting  
478 is not considered.

479 Results in the following figures are averages of at least five independent  
480 simulations, each of which simulating at least  $10^5$  requests. Since the two  
481 topologies generate relatively consistent performance results, unless other-  
482 wise specified, we present only the results obtained using the NSFnet topol-  
483 ogy for comparisons and discussions.

#### 484 4.2. Comparison of LF-SSP to the Existing Sub-wavelength Level CL-SSP 485 Method

##### 486 4.2.1. Comparisons in port-unlimited network

487 Figure 5 compares the LF-SSP method to the existing CL-SSP method  
488 in a port-unlimited network under various traffic loads for sub-wavelength-  
489 level multicast request protection. It is evident that LF-SSP consistently  
490 outperforms CL-SSP throughout the entire range of traffic loads: under low  
491 traffic loads, e.g.,  $\rho = 65$  Erlangs, LF-SSP is superior to CL-SSP by more  
492 than three orders of magnitude, whereas under higher traffic loads, e.g.,  $\rho =$   
493 110 Erlangs, LF-SSP remains superior to CL-SSP by approximately 49.1%  
494 in terms of the network BBR.

##### 495 4.2.2. Comparisons in port-limited network

496 Figure 6 presents a comparison between LF-SSP and CL-SSP in a port-  
497 limited network, where  $r = 0.6$  for all network nodes, under various traffic  
498 loads. The results illustrate that LF-SSP again reliably outperforms CL-SSP  
499 throughout the entire range of traffic loads in the request grooming process.  
500 Specifically, when the traffic load is low, e.g.,  $\rho = 60$  Erlangs, LF-SSP is

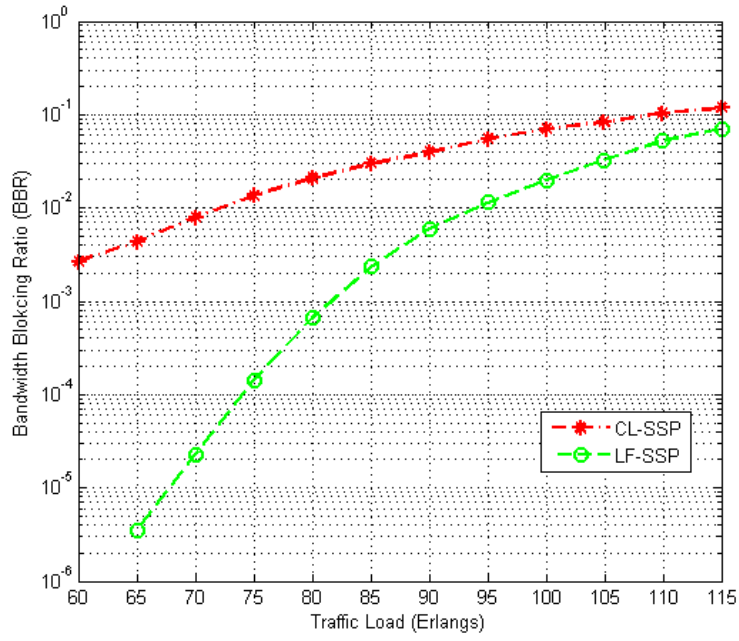


Figure 5: LF-SSP compared to CL-SSP in the port-unlimited NSFnet topology under various traffic loads ( $r = 1.0$ ).

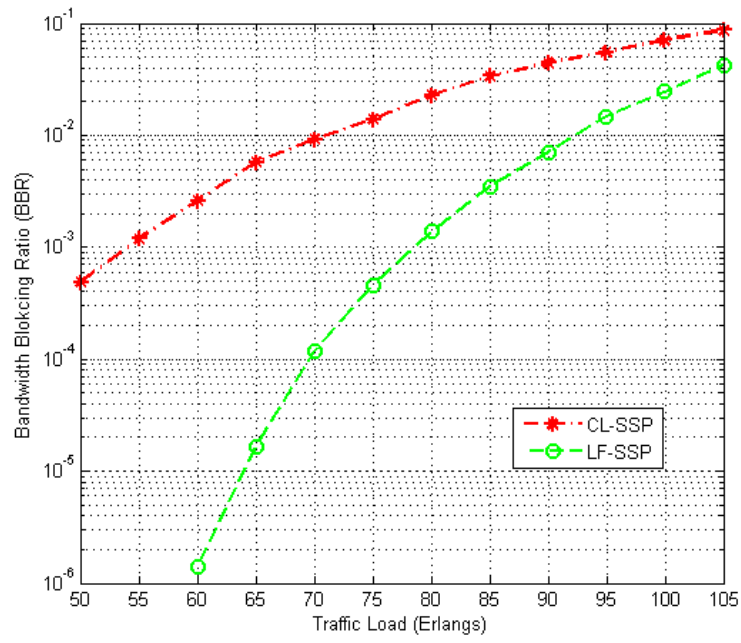


Figure 6: LF-SSP compared to CL-SSP in the port-limited NSFnet topology under various traffic loads ( $r = 0.6$ ).

superior by more than three orders of magnitude, whereas under higher traffic loads, e.g.,  $\rho = 100$  Erlangs, it outperforms CL-SPP by approximately 65.2%.

The results presented above in both Fig. 5 and Fig. 6 convincingly demonstrate that LF-SSP is able to achieve satisfactory performances in networks with either limited or unlimited port resources under different traffic loads. Such observation is due to the fact that, compared to CL-SSP, LF-SSP utilizes the LF method more conservatively in splitting new primary lightpaths in order to minimize the total resources allocated for routing and protecting a new request, and hence allowing more efficiently utilization of network resources.

To evaluate the resource utilization of LF-SSP, we define a new metric, the average utilization of existing lightpath channel capacity, which is defined as the ratio of the total traffic loads carried by the network to the total capacities of all the existing channels. Figure 7 presents the values of this metric for both methods in the port-limited NSFnet topology under various traffic loads. It is evident that the greedy segmentation of primary lightpaths in CL-SSP leads to lower wavelength utilization. The LF-SSP method, by using the LF method more carefully, improves the channel capacity utilization by approximately 15% on average. Such improvements justify the extra computations needed by the segment protection calculations in Procedure III.

#### 4.3. Comparison of LF-SSP versus the Existing Wavelength-Level SPT and LP Methods

Since there exist rather limited existing results for SMTG, to further assess the performance of the LF-SSP method, we have to extend its applications to the protection of wavelength-level multicast request protection (though it was not designed for such applications), and compare its performance versus those of the two best existing methods, namely SPT and LP, in various cases.

##### 4.3.1. Comparisons in port-unlimited network

Figure 8 compares LF-SSP to SPT and LP in the port-unlimited NSFnet topology under various traffic loads. It is evident that LF-SSP consistently outperforms both SPT and LP methods throughout the entire range of traffic loads. Specifically, when under low traffic loads, i.e.,  $\rho < 45$  Erlangs, LF-SSP outperforms LP by approximately one order of magnitude, and outperforms SPT by about 83.6%; whereas when under higher traffic loads, e.g.,  $\rho = 70$

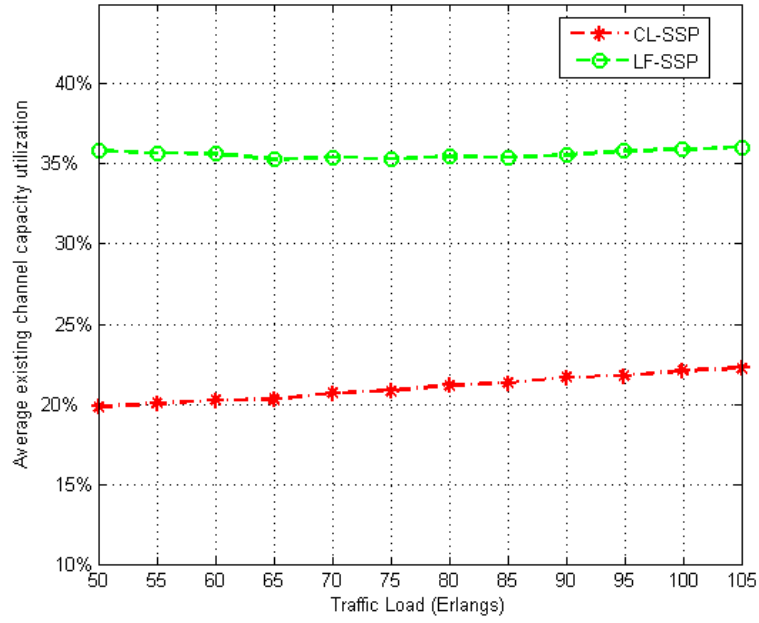


Figure 7: The average utilization of existing channel capacity versus the traffic load in the port-limited NSFnet topology ( $r = 0.6$ ).



537 Erlangs, the performances of LF-SSP is still slightly better than those two  
 538 methods. Such results can be understood: when the traffic load is low, the  
 539 network resources are relatively abundant, and thereby, the method that  
 540 is able to make more efficient usage of network resources can easily stand  
 541 out; when the traffic load is high, however, the wavelength resources are  
 542 rather limited, and consequently the differences between the performances of  
 543 different methods become less significant.

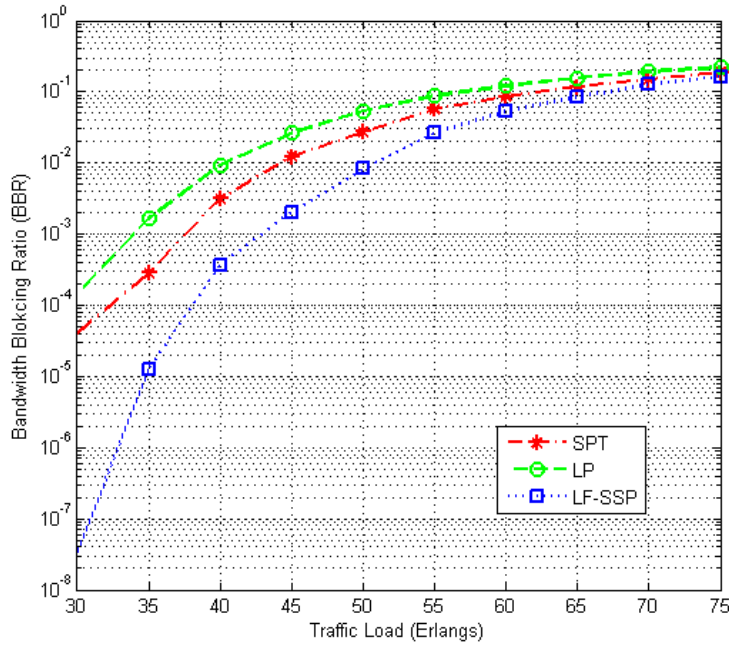


Figure 8: LF-SSP compared to the SPT and LP methods in the port-unlimited NSFnet topology under various traffic loads ( $r = 1.0$ ).

#### 544 4.3.2. Comparisons in port-limited network

545 Figure 9 compares LF-SSP against both SPT and LP in the port-limited  
 546 NSFnet topology under various traffic loads. Again we can see that, LF-SSP  
 547 evidently achieves better performance than both algorithms throughout the  
 548 entire range of traffic loads: when under low traffic loads, e.g.,  $\rho = 45$  Erlangs,  
 549 it outperforms LP by more than one order of magnitude, and outperforms  
 550 SPT by more than 80%; whereas when under higher traffic loads, e.g.  $\rho = 70$   
 551 Erlangs, performance of LF-SSP is still slightly better than those of SPT

and LP methods. Such observation is due to the fact that when the traffic load is low, the network resources are relatively abundant, and thus LF-SSP is able to fragment the new lightpaths to improve resource sharing in protection process; whereas when the traffic load is high, both the wavelength and transceiver resources become exhausted, which cause connection requests to be blocked even under best utilizations. Consequently the performance superiority of the LF-SSP method becomes less significant.

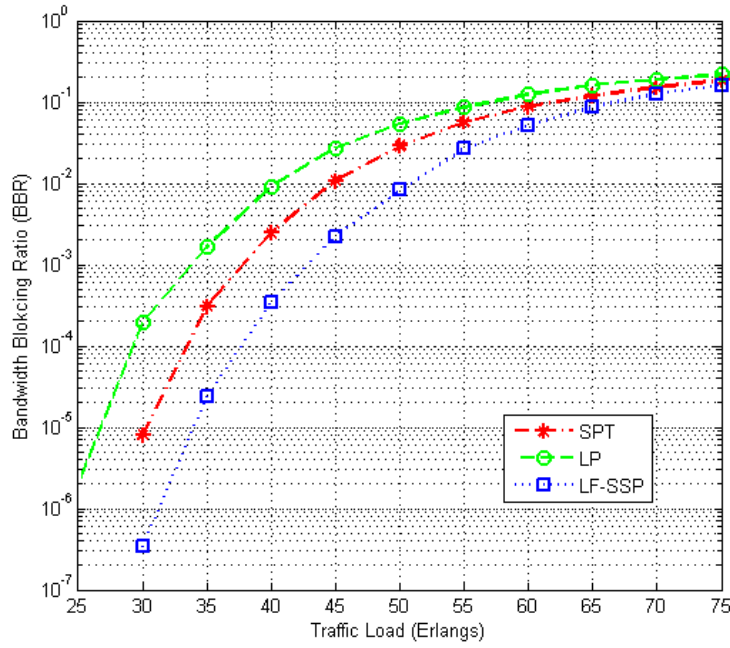


Figure 9: LF-SSP compared to the SPT and LP methods in the port-limited NSFnet topology under various traffic loads ( $r = 0.6$ ).

The results in Fig. 8 and Fig. 9 illustrate that LF-SSP is able to achieve satisfactory performance even when it is used to protect wavelength-level multicast requests. It is also interesting to note that a comparison between Fig. 8 and Fig. 9 indicates that LF-SSP performs better when the port resources are more abundant. This finding can be attributed to the fact that LF-SSP is designed to make efficient utilization of transceiver resources to minimize the network BBR.

Below, by comparing LF-SSP with a few existing methods in various cases, we assess the effects of a few factors on the LF-SSP performance.

568 4.4. Effects of the Add/drop Port Resources on Sub-wavelength and Wave-  
569 length Level Protection

570 Figure 10 illustrates a comparison between LF-SSP and CL-SSP in the  
571 NSFnet network with various port resources for SMTG. We see that, when  
572 the port resources are too limited, i.e.,  $r < 0.2$ , the performance differences  
573 between the two methods are not so big, whereas when the port resources  
574 increase to allow  $r > 0.3$ , the performance of LF-SSP improves rapidly and  
575 exceeds that of CL-SSP by more than one order of magnitude. When the port  
576 resources become relatively abundant, e.g.,  $r > 0.7$ , LF-SSP outperforms CL-  
577 SSP by nearly two orders of magnitude.

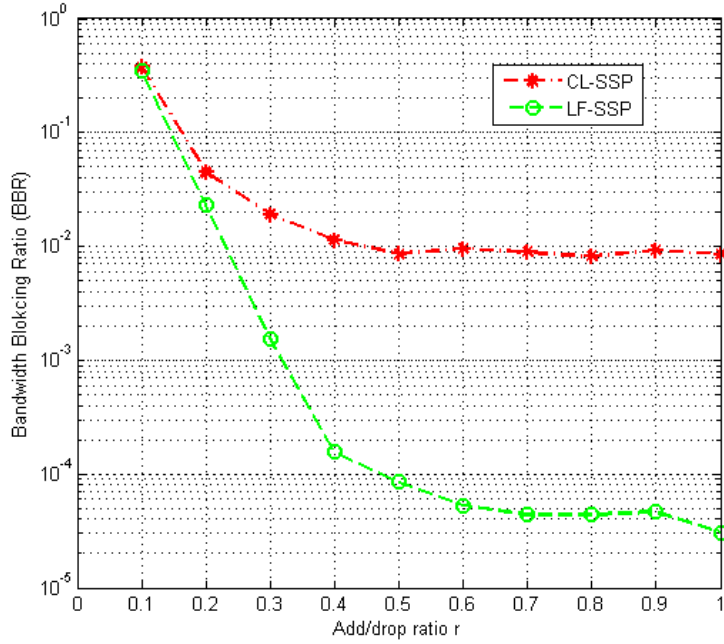


Figure 10: Comparison between LF-SSP and CL-SSP in terms of the add/drop ratio in the NSFnet topology for sub-wavelength-level request protection (traffic load  $\rho = 70$  Erlangs).

578 Figure 11 compares LF-SSP to SPT and LP for protection of wavelength-  
579 level multicast requests in NSFnet network with different add/drop resources.  
580 It is again clear that, when the port resources are limited, i.e.,  $r < 0.35$ , the  
581 BBR performances of these methods are not very different from one another.  
582 Whereas when the port resources are not so bottlenecked, e.g.,  $r > 0.35$ , the

583 BBR performance of LF-SSP improves and supersedes those of SPT and LP;  
 584 when  $r > 0.5$ , LF-SSP is superior to LP by nearly two orders of magnitude,  
 585 and outperforms SPT by approximately one order of magnitude.

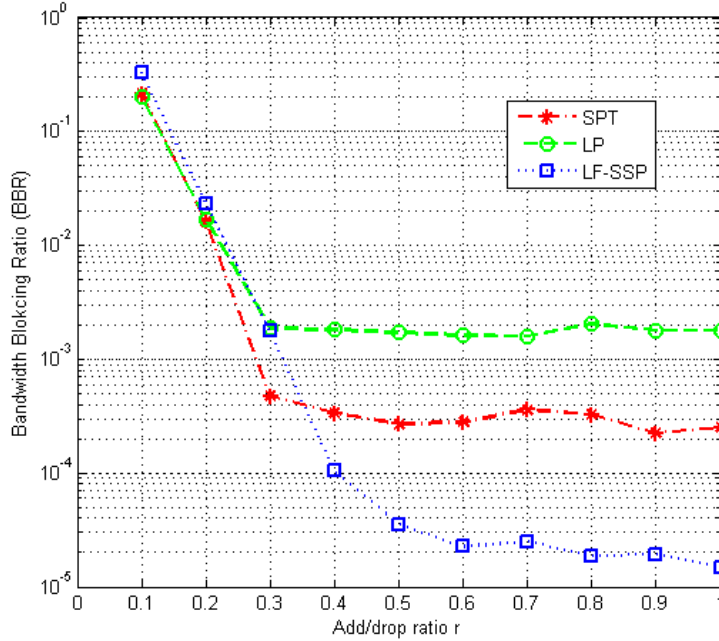


Figure 11: LF-SSP compared to the SPT and LP methods in terms of the add/drop ratio in the NSFnet topology for wavelength-level multicast request protection (traffic load  $\rho = 35$  Erlangs).

586 Such comparisons clearly demonstrate that by utilizing the LF method  
 587 to minimize the amount of resources allocated for protection of each request,  
 588 LF-SSP is able to achieve satisfactory performances for both wavelength- and  
 589 sub-wavelength-level multicast request protections as long as the transceiver  
 590 resources on the network nodes are not too limited. More redundant  
 591 transceiver resources basically lead to more significant performance superiority  
 592 of the LF-SSP method.

#### 593 4.5. Effects of the Averaged Number of Destinations of Each Request

594 We also study the influences of the average number of destinations per  
 595 multicast session on the performance of the LF-SSP method. Once again,  
 596 we consider different cases of wavelength- and sub-wavelength-level multicast

597 requests protection in networks with limited and unlimited port resources  
 598 respectively. As the conclusions hold for networks with either un-limited or  
 599 limited port resources, we present only the results obtained in port-limited  
 600 networks.

601 Figure 12 compares LF-SSP and CL-SSP in the port-limited NSFnet  
 602 topology for SMTG. Simulation results show that LF-SSP outperforms CL-  
 603 SSP: when the average size of the multicast sessions is small, e.g.,  $E(N) <$   
 604 4.5, LF-SSP is superior to CL-SSP by more than one order of magnitude;  
 605 when the size of the multicast session increases, the performance difference  
 606 between these two methods decreases. This observation can be understood:  
 607 when the size of the average multicast-session is small, the network resources  
 608 are relatively abundant and thus the performance superiority of LF-SSP is  
 609 more significant. When the average session size is large, however, the net-  
 610 work resources become relatively scarce, which decreases the performance  
 611 superiority of LF-SSP method, as we discussed earlier.

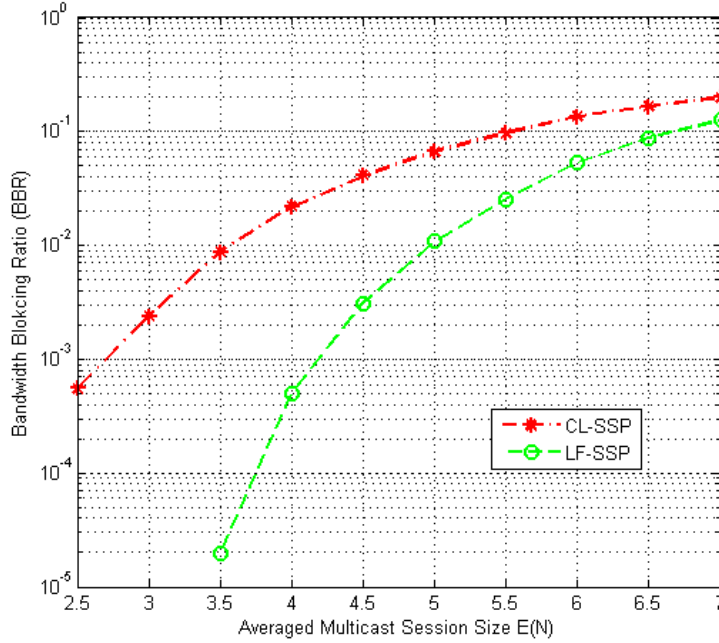


Figure 12: LF-SSP compared to CL-SSP for sub-wavelength-level multicast request protection in the NSFnet topology ( $r = 0.6, \rho = 60Erlangs$ ).

612 Figure 13 compares LF-SSP versus the SPT and LP methods for the

613 protection of wavelength-level multicast requests in the port-limited NSFnet  
 614 topology. It is evident that LF-SSP achieves better BBR performance than  
 615 both SPT and LP in the simulated cases. Specifically, when the multicast-  
 616 session size is small, i.e.,  $E(N) < 4$ , LF-SSP outperforms LP by about an  
 617 order of magnitude. Even when the average multicast-session size is larg-  
 618 er, i.e.,  $E(N) > 4.5$ , it still outperforms LP by 54% averaged over all the  
 619 simulated cases. When compared to the SPT method, LF-SSP also achieves  
 620 much better performances in different cases: when  $E(N) < 4$ , it outperforms  
 621 SPT by more than 60%; while when  $E(N) > 4.5$ , its performance is still  
 622 slightly better over that of SPT. As we have discussed earlier: more redun-  
 623 dant network resources allow the LF-SSP method to achieve more significant  
 624 improvements over the existing methods.

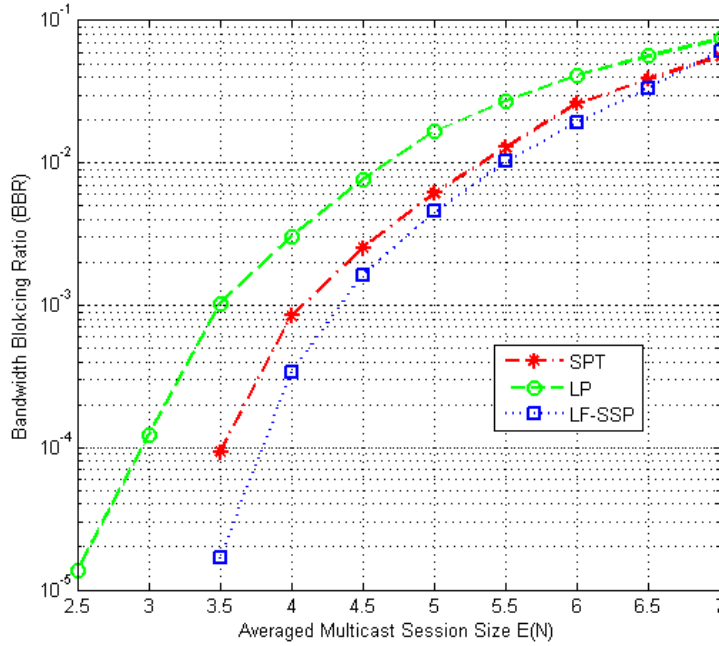


Figure 13: LF-SSP compared to SPT and LP for wavelength level multicast request protection in the NSFnet topology ( $r = 0.6, \rho = 30Erlangs$ ).

625 It is worth noting that the LF-SSP method is designed for sub-wavelength  
 626 level request protection. For wavelength-level request protection, there may  
 627 still be nontrivial space for further improving the performance of the algorithm.  
 628 For example, the three parameters defined in (4) – (6) may be optimized

629 to further improve the network resources sharing for wavelength-level request  
630 provisioning. Detailed discussions on such possible improvements, however,  
631 are out of the scope of this paper and hence, have to be left to a future report.

## 632 5. Conclusion

633 In this paper, we addressed the problem of protecting sub-wavelength-  
634 level multicast requests against single link failure in dynamic traffic groom-  
635 ing process. An efficient mechanism, namely, lightpath-fragmentation based  
636 segment shared protection (LF-SSP), was proposed. LF-SSP attempts to  
637 minimize the network BBR by adopting the LF method to properly split the  
638 primary/backup lightpaths to improve resource sharing. Extensive simula-  
639 tions have been conducted to evaluate the performances of LF-SSP in various  
640 cases. Results demonstrated that LF-SSP is capable of achieving satisfactory  
641 BBR performances for either sub-wavelength- or wavelength-level multicast  
642 request protection in networks with limited or unlimited transceiver resources  
643 under various traffic loads; performance superiority of LF-SSP compared to  
644 the existing methods is more significant when the network resources are rel-  
645 atively more abundant. The influences of variations in the number of ad-  
646 d/drop ports and average multicast destination numbers per request on the  
647 performances of LF-SSP were also evaluated.

648 Our future studies may include optimizing the algorithm for wavelength-  
649 level multicast protection, and extending the algorithm to handle the case  
650 with certain kinds of node failures, etc.

## 651 References

- 652 [1] B. Mukherjee, *Optical WDM Networks*. New York, USA: Springer Sci-  
653 ence+Business Media, Inc., 2006.
- 654 [2] I. Chlamtac, A. Ganz, and G. Karmi, "Lightpath communications: an  
655 approach to high bandwidth optical WAN's," *IEEE Trans. Commun.*,  
656 vol. 40, no. 7, pp. 1171–1182, Jul. 1992.
- 657 [3] G. N. Rouskas and H. G. Perros, "A tutorial on optical networks," *NET-*  
658 *WORKING 2002 Tutorials, LNCS 2497*, pp. 155–193, May 2002.
- 659 [4] L. H. Sahasrabuddhe and B. Mukherjee, "Light-trees: Optical multicas-  
660 ting for improved performance in wavelength-routed networks," *IEEE*  
661 *Commun. Mag.*, vol. 37, no. 2, pp. 67–73, Feb. 1999.

- 662 [5] K. Zhu and B. Mukherjee, "Traffic grooming in an optical WDM mesh  
663 network," *IEEE J. Sel. Areas Commun.*, vol. 20, no. 1, pp. 122–133, Jan.  
664 2002.
- 665 [6] N. K. Singhal, L. H. Sahasrabudde, and B. Mukherjee, "Optimal mul-  
666 ticast of multiple light-trees of different bandwidth granularities in  
667 a WDM mesh network with sparse splitting capabilities," *IEEE/ACM*  
668 *Trans. Netw.*, vol. 14, no. 5, pp. 1104–1117, Oct. 2006.
- 669 [7] A. E. Kamal, "Algorithms for multicast traffic grooming in WDM mesh  
670 networks," *IEEE Commun. Mag.*, vol. 44, no. 11, pp. 97–105, Nov. 2006.
- 671 [8] R. Lin, W.-D. Zhong, S. K. Bose, and M. Zukerman, "Light-tree configu-  
672 ration for multicast traffic grooming in WDM mesh networks," *Photonic*  
673 *Netw. Commun.*, vol. 20, no. 2, pp. 151–164, Oct. 2010.
- 674 [9] X. Yu, G. Xiao, and T.-H. Cheng, "Dynamic multicast traffic grooming  
675 in optical wdm mesh networks: Lightpath vs light-tree," *IEEE/OSA J.*  
676 *OPT. COMMUN. NETW.*, vol. 5, no. 8, pp. 870–880, Aug. 2013.
- 677 [10] S. Ramamurthy and B. Mukherjee, "Survivable WDM mesh networks.  
678 II - restoration," in *Proc. IEEE International Conference on Communi-*  
679 *cations '1999*, vol. 3, Jun. 1999, pp. 2023 – 2030.
- 680 [11] S. Ramamurthy and B. Mukherjee, "Survivable WDM mesh networks.  
681 part I-protection," in *Proc. Eighteenth Annual Joint Conference of the*  
682 *IEEE Computer and Communications Societies INFOCOM '99*, vol. 2,  
683 Mar. 1999, pp. 744 – 751.
- 684 [12] H. Drid, B. Cousin, M. Molnar, and S. Lahoud, "A survey of surviv-  
685 ability in multi-domain optical networks," *Computer Communications*,  
686 vol. 33, no. 8, pp. 1005–1012, May 2010.
- 687 [13] N. K. Singhal, L. H. Sahasrabudde, and B. Mukherjee, "Provisioning of  
688 survivable multicast sessions against single link failures in optical WDM  
689 mesh networks," *IEEE/OSA J. Lightw. Technol.*, vol. 21, no. 11, pp.  
690 2587–2594, Nov. 2003.
- 691 [14] H. Luo, L. Li, and H. Yu, "Algorithm for protecting light-trees in surviv-  
692 able mesh wavelength-division-multiplexing networks," *Journal of Optical*  
693 *Networking*, vol. 5, no. 12, pp. 1071–1083, Dec. 2006.



- [15] H. Luo, L. Li, H. Yu, and S. Wang, "Achieving shared protection for dynamic multicast sessions in survivable mesh WDM networks," *IEEE J. Sel. Areas. Commun.*, vol. 25, no. 9, pp. 83–95, Dec. 2007.
- [16] X. Wang, L. Guo, L. Pang, J. Du, and F. Jin, "Segment protection algorithm with load balancing for multicasting WDM mesh networks," in *10th International Conference on Advanced Communication Technology 2008. (ICACT 2008.)*, vol. 3. IEEE, 2008, pp. 2013–2016.
- [17] F. Zhang and W.-D. Zhong, "Performance evaluation of optical multicast protection approaches for combined node and link failure recovery," *IEEE/OSA J. Lightw. Technol.*, vol. 27, no. 18, pp. 4017–4025, Sep. 2009.
- [18] L. Long and A. E. Kamal, "Tree-based protection of multicast services in WDM mesh networks," in *Global Telecommunications Conference, 2009. GLOBECOM 2009. IEEE*. IEEE, Nov. 2009, pp. 1–6.
- [19] T. Panayiotou, G. Ellinas, and N. Antoniadis, "Segment-based protection of multicast connections in metropolitan area optical networks with quality-of-transmission considerations," *IEEE/OSA J. OPT. COMMUN. NETW.*, vol. 4, no. 9, pp. 692–702, Sep. 2012.
- [20] C. Lu and L. Li, "Dynamic multicast traffic grooming for survivable WDM mesh networks," in *Proc. International Conference on Communications, Circuits and Systems 2008*, May 2008, pp. 567–571.
- [21] C. Ou, K. Zhu, H. Zang, L. H. Sahasrabuddhe, and B. Mukherjee, "Traffic grooming for survivable WDM networks-shared protection," *IEEE J. Sel. Areas. Commun.*, vol. 21, no. 9, pp. 1367–1383, Nov. 2003.
- [22] X. Yu, G. Xiao, and T.-H. Cheng, "Connection-level segment shared protection for dynamic multicast traffic grooming," in *Proc. IEEE ICICS '2013*, Dec. 2013.
- [23] D. Xu, Y. Xiong, and C. Qiao, "Novel algorithms for shared segment protection," *IEEE J. Sel. Areas. Commun.*, vol. 21, no. 8, pp. 1320–1331, Oct. 2003.
- [24] P.-H. Ho, J. Tapolcai, and T. Cinkler, "Segment shared protection in mesh communications networks with bandwidth guaranteed tunnels,"

- 725 *IEEE/ACM Transactions on Networking*, vol. 12, no. 6, pp. 1105–1118,  
726 Dec. 2004.
- 727 [25] N. K. Singhal, C. Ou, and B. Mukherjee, “Cross-sharing vs. self-sharing  
728 trees for protecting multicast sessions in mesh networks,” *Computer Net-*  
729 *works*, vol. 50, no. 2, pp. 200–206, 2006.
- 730 [26] H. Takahashi and A. Matsuyama, “An approximate solution for the  
731 steiner problem in graphs,” *Math. Japonica*, vol. 24, no. 6, pp. 573–577,  
732 1980.
- 733 [27] X. Yu, G. Xiao, and T.-H. Cheng, “Historical data learning based dy-  
734 namic LSP routing for overlay IP over WDM networks,” *Optical Fiber*  
735 *Technology*, vol. 19, no. 4, pp. 308–319, Aug. 2013.
- 736 [28] E. A. Doumith and M. Gagnaire, “Impact of traffic predictability on  
737 WDM EXC/OXC Network performance,” *IEEE J. Sel. Areas. Commun.*,  
738 vol. 25, no. 5, pp. 895–904, Jun. 2007.