

Design of a Compact Patch Antenna Loading Periodic Jerusalem Crosses

Siya Mi^{*},¹ and Yee Hui Lee²

Abstract—A compact microstrip antenna loaded with periodic patterns etched in the ground plane is proposed. The etched patterns are Jerusalem crosses which look the same as one of the common electromagnetic band gap structures, uni-planar electromagnetic band gap. In this paper, the dielectric backed with etched ground plane is analysed in terms of metamaterial. The permittivity and permeability are derived from the simulated reflection and transmission coefficients. Then a patch is stacked on the metasubstrate, and the antenna is designed to operate at 2.4 GHz. The proposed antenna has a small dimension in comparison to two other published compact antennas. Compared to the conventional patch antenna, the proposed antenna achieves a 68.38% miniaturization of the patch, and a 2.84 times impedance bandwidth broadening. Furthermore, the operating frequency of the proposed antenna can be tuned over a large range of frequencies by physically adjusting the length of the surrounding slots or by voltage adjusting of the voltage controlled tunable inductive elements. The proposed antenna is fabricated and measured. The measurement results are found to agree well with the simulation results.

1. INTRODUCTION

Microstrip antenna is widely used because of its ease of fabrication and low cost. However, the microstrip antenna has some shortcomings caused by the substrate material. The high dielectric constant and small thickness of the substrate results in an antenna that is low gain and narrow bandwidth. The size of antenna is mainly determined by the frequency of operation and the properties of the substrate material. Take the conventional patch antenna as an example, the length of the patch is about half of the guided wavelength. In recent years, the metamaterials have received considerable attention. This is due to the special properties, which have not yet been found in nature, metamaterials are able to improve the antenna performances through the control of electromagnetic wave propagation. The metamaterials are able to address some of the shortcomings of the conventional microstrip antenna.

The metamaterial contains dealt with in this paper are uni-planar periodic structures. One of the most common metamaterial is electromagnetic band gap (EBG). It can prevent the electromagnetic wave propagation over a certain frequency range, therefore, it is often arranged around the antenna in such a way as to reduce the back lobe. EBG can also decrease the coupling between antennas in an antenna array. This can be achieved by laying EBG structures between the antenna elements of the array [1]. Frequency selective surface (FSS) is another one of the commonly used metamaterials. Working as a PEC in the operating frequency and presenting the bandpass features out of the operating frequency, FSS is able to reduce the backward scattering [2, 3, 4]. Nowadays, the metamaterial are more and more frequently used in the microstrip antenna designs to replace the traditional substrate materials [5, 6, 7]. The metasubstrate can be used to improves the operating performance of antenna, such as its radiation efficiency, gain, and impedance bandwidth.

The miniaturization of antennas, similarly, can be achieved by using metamaterials. In [8], by placing a complementary split-ring resonators (CSSR) between the patch and the ground of the antenna,

Manuscript prepared for Progress In Electromagnetics Research

* Corresponding author: Siya Mi (MiSiya@ntu.edu.sg). Co-author: Yee Hui Lee (EYHLee@ntu.edu.sg)

^{1,2} School of Electrical and Electronic Engineering, Nanyang Technological University, Singapore.

the size of the patch is significantly decreased. However, this metasubstrate is two layers, making it difficult to fabricate and doubling the thickness of this antenna. The radiation efficiency is reduced, and it is even worse this design makes the already narrow bandwidth even narrower. In [9], a microstrip antenna is miniaturized by loading a single-layer metamaterial in which four U-shaped structures are etched under the patch. This design improves both the radiation efficiency and the bandwidth, but it is a difficult to fabricate because of the vertical vias. In [10], a simple single layer patch antenna with embedded meander-line (EML) loading is proposed. This design is easy to fabricate, can reduce the patch size by about 35%, and broadens the bandwidth by 1.85 times compared to the conventional patch antenna. However, the etched EMLs allows energy leakage to the back, and thus, reducing the main lobe and gain. In order to increase the gain, a metal plane reflector is placed beneath and in parallel to the antenna ground plane. However, in order for the reflector to be effective, the distance between the reflector and the antenna ground has to be as large as 5 mm ($0.058\lambda_0$). Therefore, even though the patch size is reduced, the overall demission of the antenna still remains large, because the total thickness of the antenna is 4.2 times of the original.

In this paper, we propose to etch the periodic Jerusalem crosses in the antenna ground plane. The Jerusalem cross is one of the most common patterns which are applied in metamaterial. The Jerusalem cross can be arranged periodically to form an absorber. In [11], a multi-band absorption is effectively obtained by assembling the Jerusalem crosses. The achieved absorption rate is 96.2 % - 99.5%. In [12], the Jerusalem cross is used to design a Terahertz absorber with a near-perfect absorption. This absorber can be applied in medical imaging and communication systems. In our design, the etched Jerusalem cross is used as a metasubstrate. It can be used to reduce the size of antenna, and to improve the bandwidth. Besides performance improvement, this structure is also simple to implement and easy to fabricate. For fabrication purpose, the low cost FR4 is chosen as the substrate. Although the loss tangent of FR4 is high, the radiation efficiency is improved significantly compared to the conventional patch antenna. The improvement of maximum realized gain is small, because of energy leakage through the defects in the ground plane as explained in [10].

2. METASUBSTRATE DESIGN

The metasubstrate is constituted by a piece of dielectric backed with a ground plane etched with a 3 by 3 Jerusalem cross array. The patterned ground plane and the unit cell etched with a Jerusalem cross is shown in Fig.1. Each unit cell contains four etched patches in the centre in the form of a cross, and four etched arms attached at the end. The parameter values of the unit cell are as follows, $a = 7mm$, $l = 5.5mm$, $w = 0.4mm$, and $g = 0.25mm$. In this design, the dielectric parameter of the FR4, with ϵ_r of 4.3, and loss tangent ($\tan\delta$) of 0.025. The thickness of the substrate is 0.8 mm.

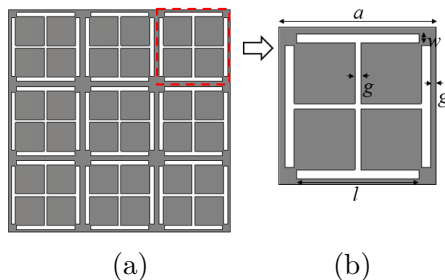


Figure 1. (a) Pattern ground plane of the metasubstrate. (b) Unit cell of the etched uni-planar compact structure. $a = 7mm$, $l = 5.5mm$, $w = 0.4mm$, and $g = 0.25mm$.

If the electrically small patterned structures are arranged in the material periodically, the metamaterial can be taken as a uniform dielectric with a certain permittivity and permeability. The effective permittivity will get smaller because of the absence of metal due to the etched pattern in the ground plane. The permittivity and permeability of the metamaterial can be derived from the transmission and reflection coefficients [13, 14]. A microstrip line on top of the metasubstrate is simulated in order to examine the properties of the metasubstrate. This structure is simulated using

CST Microwave Studio (a 3D EM simulation software), and the transmission and reflection coefficients are acquired. The impedance Z and the refractive index n can be derived from the transmission and reflection coefficients given by Eq. (1)-(3).

$$Z = \pm \sqrt{\frac{(1 + S_{11})^2 - S_{21}^2}{(1 - S_{11})^2 - S_{21}^2}} \quad (1)$$

$$n = \frac{1}{k_0 d} \{Im[\ln(e^{ink_0 d})] + 2m\pi - jRe[\ln(e^{ink_0 d})]\} \quad (2)$$

$$e^{ink_0 d} = \frac{S_{21}}{1 - S_{11} \frac{Z-1}{Z+1}} \quad (3)$$

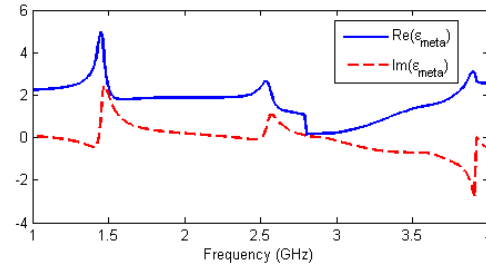
where k_0 is the wave number in free space, and $k_0 = 2\pi f/c$. d is the transmission distance between two ports, in other words, it is the length of the dielectric.

In Eq. (1), the sign of Z should be determined carefully to ensure $Re(Z) \geq 0$ and $Im(n) \geq 0$, or equivalently, $|e^{ink_0 d}| \leq 1$. In Eq. (2), m is an integer related to the real part of the refractive index, which can be determined exactly by the method in [15]. The effective permittivity and permeability of the metasubstrate can be then calculated as Eq. (4) and Eq. (5).

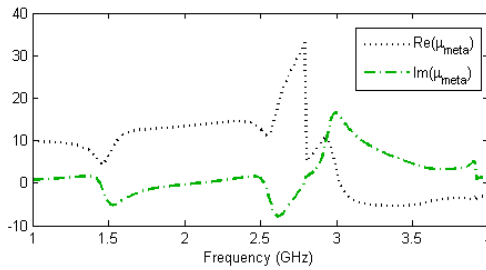
$$\epsilon_{meta} = \frac{n}{Z} \quad (4)$$

$$\mu_{meta} = nZ \quad (5)$$

The calculated permittivity is shown in Fig.2 (a). From 1 GHz to 4 GHz, the real part of ϵ_{meta} is greater than 0, and it is almost below the original permittivity ϵ_r of FR4 ($\epsilon_r = 4.3$) except at around 1.45 GHz. The low permittivity of the metasubstrate is due to the leakage of electric field from the defects in the ground plane. This effectively reduces the permittivity of the substrate. Note that the effective ϵ of the metasubstrate varies with frequency. The permeability of the substrate is plotted in Fig.2 (b). From 1 GHz to 3.0 GHz, the real part of μ_{meta} is bigger than 1 (the permeability of FR4 and air), and it falls to 0 when the frequency is larger than about 3.0 GHz. Above 3.0 GHz, the permeability being blow 0, performs like a negative permeability material. The imaginary parts of ϵ_{meta} and μ_{meta} indicates that there is leakage loss of the gap in the ground.



(a)



(b)

Figure 2. (a) The permittivity of the metasubstrate. (b) The permeability of the metasubstrate.

3. ANTENNA DESIGN

The patch of the antenna is designed as a simple square patch. The length of the patch is the half of the wavelength in metasubstrate. This is calculated using Eq. (6) [16]. An antenna operating at 2.4 GHz will be designed. In Fig.2, the permittivity and permeability of the metasubstrate at 2.4 GHz can be determined to be 1.9 and 14.4, respectively. The imaginary parts are ignored, since they are very small, which indicates that the loss is negligible. Even through the permittivity of the metasubstrate is less than 4.3, the length of the patch is reduced due to the dominant increase in the permeability of the metasubstrate, μ_{eff} . The practical length of the patch should be longer because of the fringing effect. Based on the theory and simulation, the length of the patch is determined to be 16.7 mm for an operating frequency of 2.4 GHz.

$$L = \frac{c}{2\pi f \sqrt{\epsilon_{eff}\mu_{eff}}} \quad (6)$$

In this design, the periodic pattern is arranged only beneath the patch to allow for ease of the impedance matching. A 3×3 array of unit cell patterns is etched in the ground plane. Each unit is as shown in Fig.1 (b). There is energy leakage from the defects in the plane ground, so the back lobe is increased regardless of the size of the ground plane. Therefore, the ground plane size is kept at $22mm \times 40mm$. On the top side, a 50 ohm microstrip insert feed line is used to feed the patch antenna and also to achieve the impedance matching. The insert depth is calculated to be 9 mm. The top and bottom view of the proposed antenna is as shown in Fig.3.

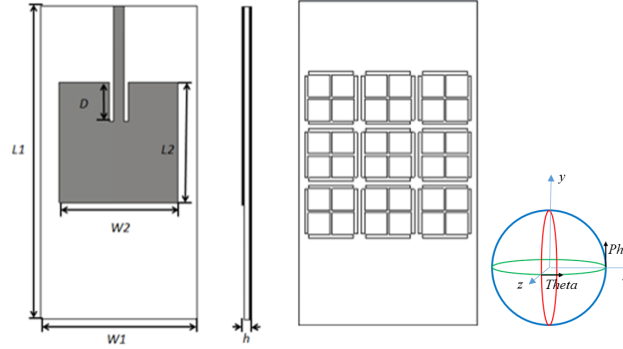


Figure 3. The illustration of microstrip antenna.

4. RESULTS AND DISCUSSION

4.1. Simulated Results

The proposed antenna is simulated by CST studio. A conventional patch antenna, which also operates at 2.4 GHz and uses the same FR4 PCB as the substrate, is simulated for comparison purposes. The reflection coefficients of both simulated antennas are shown in Fig.4. The solid line and dash dot line are the simulated reflection coefficient of the antennas using metasubstrate and conventional dielectric, respectively. The -10 dB impedance bandwidth of the antenna using metasubstrate is about 7.1%, while the bandwidth of the conventional patch antenna is only 2.5%. The quality factor is proportional to the permittivity of the substrate, and is inversely proportional to the permeability as shown in Eq. (7).

$$Q = \frac{\pi w_p \sqrt{\epsilon_{eff}}}{2G_r h \eta_0 \sqrt{\mu_{eff}}} \quad (7)$$

where G_r is the radiation conductance. η_0 is the electromagnetic wave impedance in free space. Thus, by decreasing ϵ_{eff} and increasing μ_{eff} , the Q factor of the antenna becomes smaller, and the bandwidth gets broader.

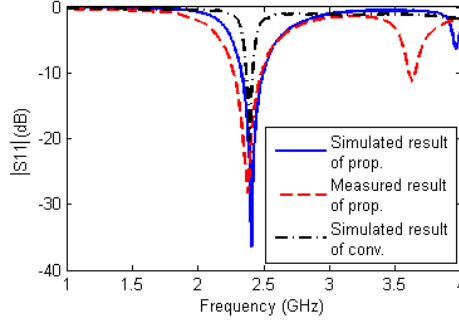


Figure 4. The simulated and measured return loss.

The radiation patterns of the proposed antenna are plotted in Fig.5. From the radiation patterns, it can be seen that some energy leakage to the back through the patterns etched in the ground plane is observed in the form of an increasing in the back lobe of the antenna. The directivity of this antenna gets smaller, and it looks like an omni-directional antenna. The dimension and radiation performance of the proposed antenna and the conventional patch antenna are listed in Table.1.

Table 1. Comparison of the antenna using metasubstrate and the conventional patch antenna.

	Patch Size (mm^2)	Bandwidth	Radiation Efficiency
Metasubstrate Antenna	16.7×16.7	7.1%	88.5%
Conventional Antenna	29.7×29.7	2.5%	46.3%

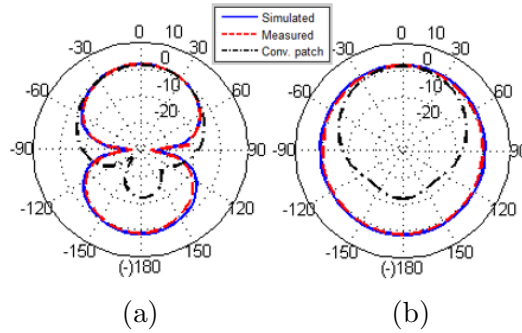


Figure 5. The simulated and measured radiation pattern. (a) E-plane. (b) H-plane.

In Table. 1, the radiation efficiency is high, at 88.5%, while the radiation efficiency of the conventional patch antenna is only 46.3% because of the high tangent loss of the FR4 dielectric substrate. The radiation efficiency takes into consideration the reflection, conduction, and dielectric losses. The efficiency is defined as the ratio of the power radiating out to the total delivered power [16], so the efficiency is in Eq. (8).

$$e = \frac{R_r}{R_r + R_L} \quad (8)$$

where R_r is the radiation resistance, and it represents the radiation by the antenna. R_L is the conduction and dielectric losses. With periodic patterns etched in the ground plane, the size of the patch gets smaller, and the radiation resistance is increased. Thus, based on Eq.8, the radiation efficiency of the antenna is improved.

4.2. Fabrication and Measured Results

The antenna with metasubstrate is fabricated. Without any vertical vias and connectors, this one-layer antenna is very easy to fabricate and can be done using the common PCB milling machine. The photos of the fabricated antenna are shown in Fig. 6 (a). In order to visualise the significant difference in the dimensions of the antenna and the proposed metasubstrate patch antenna, both operating at 2.4 GHz, are placed together and compared in Fig.6 (b). It is easy to see that the proposed antenna is able to achieve a significant reduction in antenna size. The proposed compact antenna is also compared with some of the small size antennas introduced in section 1. Their dimensions are listed in Table 2. Compared with the conventional patch antenna and the two published small size antennas, the proposed antenna has the smallest dimension.

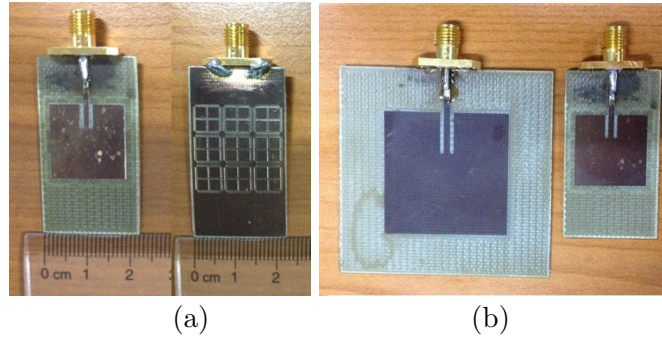


Figure 6. The photos of microstrip antenna. (a) The top view and back view of proposed antenna. (b) The proposed antenna vs. the conventional patch antenna.

Table 2. Comparison of the antenna using various metamaterials.

Antenna (Reference)	Unite Cell of Metamaterial	Antenan Size
Proposed	UC-EBG	$0.17\lambda_0 \times 0.32\lambda_0 \times 0.006\lambda_0$
[9]	Inverted U shape	$0.17\lambda_0 \times 0.32\lambda_0 \times 0.030\lambda_0$
[10]	Embedded meander line	$0.70\lambda_0 \times 0.89\lambda_0 \times 0.017\lambda_0$

The compact antenna is measured in an anechoic chamber. The measured S-parameter and radiation pattern are plotted and compared with the simulated ones in Fig.4 and Fig.5, respectively. The measured results and the simulated results agree well with each other.

4.3. Frequency Tuning

The flexibility of operating frequency tuning is one of the most important issues to determine the performance of an antenna [17]. In our proposed design, the resonance frequency can be tuned conveniently by changing the arm slots of length, l , as shown in Fig.1 (b). By changing the arm slot length, l , the effective permittivity and permeability of the metasubstrate can be varied. It is a common practice to adjust the size or the frequency of operation of the antenna by changing the effective permittivity or permeability of the substrate.

In this design, when l is increased from 0.5 mm to 5.5 mm in steps of 1 mm, while keeping the other parameters constant as those listed in Fig.1, the resonance frequency can be tuned from 3.74 GHz to 2.4 GHz. The tuning frequency range is large. In Fig.7, it can be seen that the impedance match is good, and the return loss is better than -17 dB for varying lengths of l even with the unchanged depth of the insert feed. The radiation pattern of the tunable antenna is also stable. In Fig.8, the radiation patterns of the antenna with three different resonant frequency, corresponding to three values of l are plotted. With varied length of the connecting arms, the radiation pattern is almost unchanged except

for the back lobe. However, this can be expected as the back lobe is determined by the amount of leakage through the ground plane. Therefore, the smallest arm length, l , results in the smallest back lobe and vice versa.

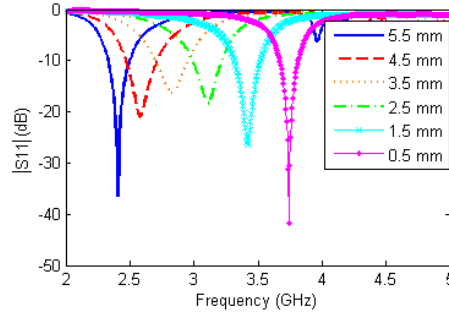


Figure 7. The dependence of reflection coefficients on parameter l .

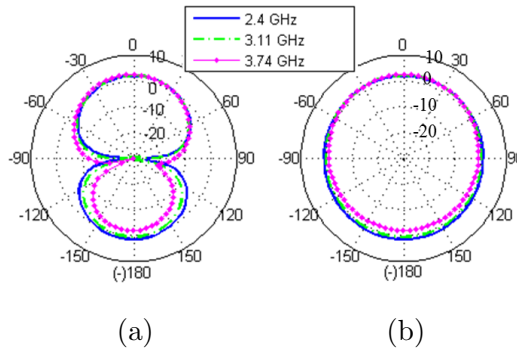


Figure 8. The radiation patterns with varied l . (a) E-plane. (b) H-plane.

However, the physical dimension of the slot can only be adjusted through re-fabrication. Therefore, we explore the possibility of using lump components for the tuning of the operation frequency of the antenna. Note that this technique is also employed in the implementation of the reconfigurable frequency selective surfaces [18].

Changing the length of the connecting arm, l , equals to change the equivalent inductance of it. One of the simplest method to vary the equivalent inductance is to use tunable inductive elements (eg. PIN diodes). By adjusting the voltage, the value of the inductance is changed, and the operating frequency is also changed. In Fig.9, the etched ground plane with diodes is shown. In order to tune the frequency, the tunable inductor is placed in parallel with the inductive arm with length of l as shown in Fig.9.

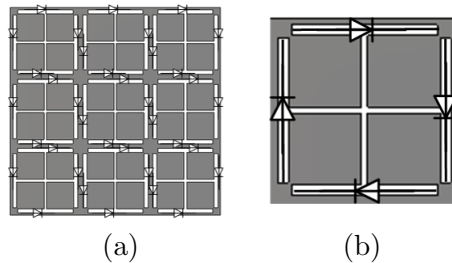


Figure 9. The equivalent circuit of the tunable antenna. (a) the pattern in the ground plane. (b) one unit cell with diodes.

When the tunable inductor is adjusted from 100 nH to 1 nH, the operating frequency of the antenna can be tuned from 2.33 GHz to 2.62 GHz. Even through the tunable inductors can vary the equivalent

inductance, its effect on the electromagnetic wave propagation properties of the structure in the ground is not as significant as the physical variation in the length of the arm slot. Thus, the frequency range tuned by the lumped elements is not as significant as the frequency range tuned by the change in physical length of the arms. The simulated results are as shown in Fig.10. Note the impedance match is kept well. In Fig.11, the radiation patterns of the antenna with tunable inductors are plotted. When the inductance equals to 1 nH and 100 nH, the radiation patterns are almost the same with no variation in the size of the back lobe at the corresponding resonant frequency. That is because, when the inductance is tuning, the physical shape and dimension of this antenna and slots remains unchanged.

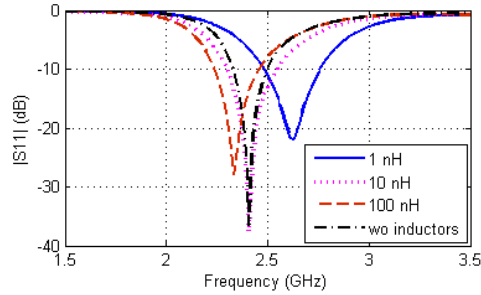


Figure 10. The simulated result of the tunable antenna.

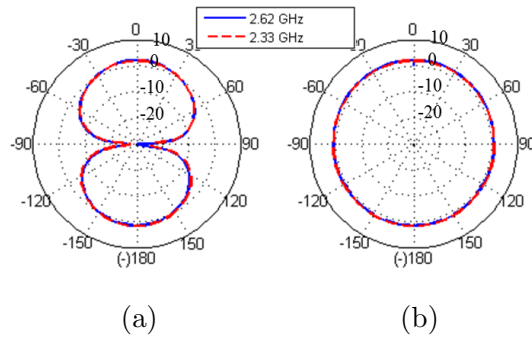


Figure 11. The radiation patterns with varied inductance. (a) E-plane. (b) H-plane.

5. CONCLUSION

In this paper, a compact microstrip antenna is designed. The patch of the antenna is stacked on a metasubstrate with periodic patterns etched in the ground plane. The effective permittivity and permeability of this metasubstrate is calculated from the simulated reflection and transmission coefficients. With the defects in the ground plane, the effective permittivity, ϵ_{meta} , of the metasubstrate gets smaller, while the effective permeability, μ_{meta} becomes much greater. Due to the small permittivity and large permeability change of the substrate, the size of the patch is decreased to 31.62%, and the impedance bandwidth is increased to 2.84 times of those of the conventional patch antenna. Even though the energy leakage through the defects in the ground plane is significant, the maximum realized gain is increased by 0.37 dB, and the radiation efficiency is improved from 39.5% to 88.5%. Furthermore, The operating frequency of this design can be tuned over a large frequency range, from 2.4 GHz to 3.74 GHz by adjusting the length of the arm slot of the pattern etched in the ground plane. If this antenna is to be used as a tunable antenna, an voltage controlled tunable inductive element can be added across (in parallel with) the arm slot. By doing so, the antenna can be tuned from 2.33 GHz to 2.62 GHz. In this paper, a small size, high performance metasubstrate antenna is proposed. This antenna can easily be fabricated and can easily be tuned and/or made tunable.

REFERENCES

1. Yang, F. and Y. Rahmat-Samii, "Microstrip antennas integrated with electromagnetic band-gap (EBG) structures: a low mutual coupling design for array applications," *IEEE Transactions on Antennas and Propagation*, Vol. 51, No. 10, 2936–2946, 2003.
2. Li, H., Wang, B.Z, Zheng, G., and Shao, W., "A reflectarray antenna backed on FSS for low RCS and high radiation performances," *Progress In Electromagnetics Research C*, Vol. 15, 145–155, 2010.
3. Jia, Y., Liu, Y., Wang, H., Li, K, and Gong, S., "Low-RCS high-gain and wideband mushroom antenna," *IEEE Antennas Wireless Propagation Letter* , Vol. 14, 277–280, 2015.
4. Kim, S.-H, Nguyen, T.T., and Jang, J.-H, "Reflection characteristics of 1-D EBG ground plane and its application to a planar dipole antenna," *Progress In Electromagnetics Research*, Vol. 120, 51–66, 2011.
5. Xu, H.-X, Wang, G.-H, and Qi, M.-Q., " A miniaturized triple-band metamaterial antenna with radiation pattern selectivity and polarization diversity," *Progress In Electromagnetics Research*, Vol. 137, 275–292, 2013.
6. Wu, B.-I, Wang, W., Pacheco, J., Chen, X., Crzegorzcyk, T., and Kong, J.A., "A study of using metamaterials as antenna substrate to enhance gain," *Progress In Electromagnetics Research*, Vol. 15, 295–328, 2005.
7. Rahimi, M., Zarrabi, F.B., Ahmadian, R., Mansouri, Z., and Keshtkar, A., "Miniaturization of antenna for wireless application with difference metamaterial structures," *Progress In Electromagnetics Research*, Vol. 145, 19–29, 2014.
8. Ouedraogo, R.O., Rothwell, E.J., Diaz, A.R., Fuchi, K., and Temme, A., " Miniaturization of patch antenna using a metamaterial-inspired technique," *IEEE Transactions on Antenna and Propagation*, Vol. 60, No. 5, 2175–2182, 2012.
9. Saghanezhad, S.A.H, and Atlasbaf, Z., " Miniaturized dual-band CPW-fed antennas loaded with U-shaped metamaterials," *IEEE Antennas Wireless Propagation Letter*, Vol. 14, 658–661, 2015.
10. Yang, X.M., Sun, Q.H., Jing, Y., Cheng, Q., Zhou, X.Y., Kong, H.W., and Cui, T.J., "Increasing the bandwidth of microstrip patch antenna by loading compact artificial magneto-dielectrics," *IEEE Transactions on Antenna and Propagation*, Vol. 59, No. 2, 373–378, 2011.
11. Wang, G. D., Liu, M. H., Hu, X. W., Kong, L. H., Cheng, L. L., and Chen, Z. Q., "Multi-band microwave metamaterial absorber based on coplanar Jerusalem crosses," *Chinese Physics B*, Vol. 23, No. 1, 017802, 2013.
12. Arezoomand, A.S., Zarrabi, F.B., Heydari, S., and Gandji, N.P., "Independent polarization and multi-band THz absorber base on Jerusalem cross," *Optics Communications*, Vol. 352, 121–126, 2015.
13. Smith, D.R., Schultz, S., Markos, P., and Soukoulis, C.M., "Determination of effective permittivity and permeability of metamaterials from reflection and transmission coefficients," *Physical Review B*, Vol. 65, No. 19, 195104, 2002.
14. Hasar, U.C., Barroso, J.J., Sabah, C., Ozbek, I.Y., Kaya, Y., Dal, D. and Aydin, T., "Retrieval of effective electromagnetics parameters of isotropic metamaterials using reference-plane invariant expressions," *Progress In Electromagnetics Research*, Vol. 132, 425–441, 2012.
15. Szab, Z., Park, G., Hedge, R., and Li, E., "A unique extraction of metamaterial parameters based on Kramers-Kronig relationship," *IEEE Transactions on Microwave Theory and Techniques*, Vol. 58, No. 10, 2646–2653, 2010.
16. Balanis, C.A., *Antenna theory: analysis and design*, John Wiley and Sons, 1997.
17. Cai, T., Wang, G.-M., and Liang, J.-G., "Analysis and design of novel 2-d transmission line metamaterial and its application to compact dualband antenna," *IEEE Antennas Wireless Propagation Letter*, Vol. 13, 555–558, 2014.
18. Turpin, J.P., Werner, D.H., and Wolfe, D.E., "Design considerations for spatially reconfigurable metamaterials," *IEEE Transactions on Antenna and Propagation*, Vol. 63, No. 8, 3513–3520, 2015.