Abstract—Enabling precise forecasting of the remaining useful life (RUL) for machines can reduce maintenance cost, increase availability, and prevent catastrophic consequences. Data-driven RUL prediction methods have already achieved acclaimed performance. However, they usually assume that the training and testing data are collected from the same condition (same distribution or domain), which is generally not valid in real industry. Conventional approaches to address domain shift problems attempt to derive domain-invariant features, but fail to consider target-specific information, leading to limited performance. To tackle this issue, in this article, we propose a contrastive adversarial domain adaptation (CADA) method for cross-domain RUL prediction. The proposed CADA approach is built upon an adversarial domain adaptation architecture with a contrastive loss, such that it is able to take target-specific information into consideration when learning domain-invariant features. To validate the superiority of the proposed approach, comprehensive experiments have been conducted to predict the RULs of aeroengines across 12 cross-domain scenarios. The experimental results show that the proposed method significantly outperforms state-of-the-arts with over 21% and 38% improvements in terms of two different evaluation metrics.

Index Terms—Domain adaptation, deep learning, remaining useful life (RUL), transfer learning.
data are available for the RUL prediction task [13], [14]. These assumptions can be impractical for many real-world applications with the following reasons. First, the collection of labeled data (failures) is expensive. For some complex and critical machines, running to failure can be costly and cause catastrophic consequences [14], [15]. Furthermore, machine deterioration process may prolong up to years, which can also limit the availability of faulty data [16]. Second, the labeled data may only be available under a specific working condition, which can be leveraged to build a model for RUL prediction. However, when the working condition changes, the previously trained model often cannot work well, due to the distinct data distributions for different working conditions [13], [15], [17].

With the aforementioned problems, the RUL prediction for scarce-labeled machines/working conditions can be very challenging. Therefore, there is an urgent need for a prognostic model that is able to estimate RUL of new working conditions with no labeled data available. Domain adaptation (DA), which enables knowledge transfer from rich-labeled domain to a different but related scarce-labeled domain [17], provides a good candidate solution for this problem. Most of the existing DA algorithms are designed for the image-related tasks [18]. Recently, some approaches extended DA for fault diagnosis problems (classification problems) to classify faults among different machines or working conditions [10], [19]. However, less attention has been paid to domain adaptation for the RUL prediction, which is a typical time-series regression problem.

To promote the intelligent fault prognosis applications with unlabeled data, we propose a novel contrastive adversarial domain adaptation (CADA) approach for machine RUL prediction across different working conditions. More specifically, CADA aims to transfer the knowledge learnt from one working condition to solve the RUL prediction problem in another working condition. Generally, adversarial adaptation approaches aim to find a feature representation of the target domain that can be invariant from the source domain. The existing deep feature extractors with their large complexity can find arbitrary transformation of the target domain that can be similar to the source. However, only finding domain invariant features does not guarantee good performance on the target domain [20], [21]. Specifically, forcing target domain features to be similar to source domain features with no constraints can remove the target specific information, i.e., the mutual information between the target data and the target extracted features, which could hinder the model performance. To handle this issue, inspired by the noise contrastive estimation (NCE), we propose a novel approach that leverages the InfoNCE loss [22] to preserve the structure of the target domain features during the domain adaptation process. We jointly optimize the target feature extractor to minimize both the domain adaptation loss and the InfoNCE loss. Specifically, the domain adaptation loss guides the target feature extractor to produce source-like features, and the InfoNCE loss preserves the target specific features by maximizing the mutual information between the target input data and the target features. Maximizing the mutual information between the input space and the feature space can preserve intrinsic structure of the target data during domain alignment process, which can boost the performance of domain adaptation. We have performed extensive experiments to verify the performance of the proposed CADA method on machine RUL prediction across different working conditions.

The main contributions of this work are summarized as follows.

1) We designed a novel adversarial domain adaptation approach for challenging yet practical machine RUL prediction. This approach successfully transfers knowledge for RUL prediction from one condition (distribution/domain) to another.
2) We proposed a novel solution based on the InfoNCE loss to learn the invariant representation and preserve the original structure for the target domain. As such, satisfactory performance for the RUL prediction can be achieved.

II. RELATED WORKS

In this section, we highlight the related works in data-driven RUL prediction and domain adaptation.

A. Deep Learning for RUL Prediction

Deep learning approaches for RUL prediction can be categorized into feed-forward neural networks and recurrent neural networks [6]. For instance, Zhu et al. [8] used the CNN to extract features in multiple scales for the detection of the fault growth and the prediction of the machine RUL [8]. Liu et al. [23] proposed a CNN network with joint loss to detect fault and predict RUL concurrently. Deutch and He [9] applied a DBN to extract features and a deep neural network to predict the RUL.

The recurrent neural network (RNN) with its sequential modeling capability can be more suitable to model dynamic systems. The LSTM is one of the most popular recurrent approaches that can model long-term dependencies and tackle vanishing gradient problems of the RNN. In [11], the authors proposed a bidirectional LSTM (BiLSTM) approach with auxiliary features to predict the RUL under multiple operation conditions. Chen et al. [12] developed an attention-based LSTM approach to adaptively select important features, resulting an accurate prediction of the RUL.

B. Domain Adaptation

Most of RUL prediction methods assume the following: access to enough labeled failure information; and training data (source) and testing data (target) are drawn from the same distribution. In reality, labeled data can be scarce and marginal distribution of data can vary according to the variation of working conditions.

A subset of transfer learning named unsupervised domain adaptation (DA) is developed to address distribution shift problem of unlabeled domains. The conventional approaches for DA reweight source samples according to their similarity with target samples [24]. While other approaches aim to reduce the domain shift problem in the feature space by minimizing the divergence between the source and target features. In [25], the maximum mean discrepancy (MMD) metric was developed to mitigate
the domain shift problem. Sun et al. [26] aimed to minimize the covariance shift between the source and target features to align the two domains. Recently, adversarial domain adaptation approaches, which intend to find invariant features in both source and target domains, have achieved the state-of-the-art performance. Inspired by generative adversarial networks (GANs), adversarial adaptation entails a domain classifier to discern between the source and target features and a deep network to extract features that can fool the domain classifier. For instance, the authors in [27] proposed a reverse gradient (RevGrad) strategy to adversarially train the domain classifier and the feature extraction network. While in [28], a typical GAN loss was employed with flipped labels to find domain-invariant features. Russo et al. [29] proposed a generative domain adaptation approach to align the source and target domains. Specifically, they used a bidirectional mapping from source to target and from target to source, while using self-labeling for the target domain. Satio et al. [30] aligned distributions of the source and target domains by designing task-specific decision boundary. To achieve that, they minimized the maximum discrepancy loss between two different classifiers for the same sample. Lee et al. [31] proposed a similar approach, which attempts to replace the $L_1$-loss term with a new sliced Wasserstein distance. In [32], a teacher model was employed to generate pseudolabels for the target domain and align the source and target clusters. In [33], the authors proposed a new adversarial loss that aims to align the joint distribution explicitly. Particularly, they introduced a classifier-aware adaptation method, where the classifier has one additional neuron for the domain classification task.

Li et al. [34] developed a heterogeneous adaption approach, where the source and target have different feature space. They considered both the sample space and feature space for the domain alignment with the MMD. Then, a graph-based sample reweighting method was used to transfer knowledge on the sample space. In [35], a progressive domain alignment approach has been developed to adapt two heterogeneous domains. Specifically, a shared codebook was employed to align the feature discrepancy while progressively minimizing the domains discrepancies. In [36], the feature space and the sample space were jointly adapted to preserve the local consistency among samples. In [37], the authors designed the maximum density divergence to enforce clustering assumption while adversarially adapting the two domains.

In RUL domain, very few works have tried to address knowledge transfer problem among different domains. Zhang et al. [25] proposed a transfer learning approach for the RUL problem, where they trained the model on the source dataset and fine tuned the model on target working condition. Yet, they assumed accessibility to labeled data for the target domain, which cannot hold for real-world scenarios. Very recently, Costa et al. proposed a deep domain adaptation (DDA) method for the RUL prediction problem using unlabeled target domain data. The DDA applied the LSTM network to extract features and the reverse gradient approach to alleviate the domain shift problem [26]. Most of these approaches aim to find a domain-invariant features between the source and target domains. Yet, simply enforcing the target features to be similar to the source with no constrains may remove useful target-specific information in target domain, i.e., the mutual information between the target data and the target extracted feature. This would limit the performance of domain adaptation for the RUL prediction task.

Differently, in our method, we develop a robust adversarial domain adaptation approach that can find domain-invariant features while preserving the target-specific features. To achieve that, we propose a novel contrastive loss-based approach to maximize the mutual information between the input space and the latent space of the target data during the domain alignment. To the best of our knowledge, the proposed CADA is the first approach that realizes adversarial domain adaptation while preserving the target-specific features for RUL prediction. Specifically, the CADA can find new feature representation of the target domain data that can be similar to the source and have maximum mutual information with the target where no labeled data are available.

III. METHODOLOGY

A. Problem Formulation and Notations

To clearly formulate the problem, we introduce the basic standard notations of domain adaptation [17]. Let a domain $D = \{X, P(X)\}$, where $X$ is the feature space, $X \in \mathcal{X}$, and $P(X)$ is the marginal distribution of data in this feature space. Given a labeled source domain $D_S = \{X_S, P_S(X)\}$ and an unlabeled target domain $D_T = \{X_T, P_T(X)\}$, the unsupervised domain adaptation problem aims to transfer knowledge from the labeled source to improve the performance on the unlabeled target. In our problem, $D_S$ and $D_T$ are both multivariate time-series data of aircraft engines under different working/fault conditions. Particularly, we have labeled data from aircraft engines with a specific working/fault condition, and we aim to improve the RUL prediction of unlabeled data with different working/fault conditions. We denote the source domain $D_S = \{X^s_i, y^s_i\}_{i=1}^{n_S}$, with $n_S$ the total number of samples, where $X^s_i \in \mathbb{R}^{M \times K}$ is the input source sample with $M$ sensors and $K$ time steps, $y^s_i \in \mathbb{R}$ is the corresponding RUL label. Similarly, the unlabeled target domain $D_T = \{X^t_j\}_{j=1}^{n_T}$, where $X^t_j \in \mathbb{R}^{M \times K}$ and $n_T$ is the number of target domain samples. Table 1 summarizes the notations used in this article.

B. Overview

Domain adaptation for multivariate time-series regression can be a very challenging task. Therefore, only few works have been presented for RUL estimation problems across domains [14]. In this article, we develop a novel CADA approach for the machine RUL prediction. Specifically, it is able to transfer the knowledge learned from the data under one condition (labeled source domain) to the data from another condition (unlabeled target domain). The proposed CADA can find domain-invariant representations of the target domain data while preserving their intrinsic structure, which is crucial to achieve satisfactory performance in the target domain.

Fig. 1 shows the overall framework that presents the detailed steps of learning procedure of the CADA model. The first stage
involves data preparation for both source and target domains. In the second stage, the source and target features are extracted by the source and target encoders, respectively. Given the target features, the target encoder $E_T$ is updated to optimize both the adversarial loss and the InfoNCE loss. In the last stage, the trained target feature extractor and the trained source RUL predictor are combined to predict the RULs for the target domain data. We will provide a detailed explanation of each module in the following subsections.

### C. Supervised Pretraining on the Source Domain

In this section, we will present our approach that models the dynamics of multivariate time series and automatically extracts salient features. In addition, we will provide details about the RUL prediction network that maps from the latent features to the RUL.

#### 1) Recurrent Multivariate Modeling:

Recurrent-based approaches are widely adopted for modeling temporal dependencies of time-series data. But RNNs often suffer from the problem of vanishing gradient with long-term sequences [38]. Alternatively, the LSTM, which is a strong variant of the RNN can handle long-term dependencies and tackle vanishing gradient problem. In this work, we design a very deep bidirectional LSTM network with five successive layers for automatic and representative feature extraction. The LSTM feature extractor represents the multivariate time series to a single-vector hidden representation as shown in Fig. 2. Specifically, the LSTM network can be represented as multiple sequential feed-forward layers. The transition function between these layers is a key function to model the temporal dependence along the data, which can be formulated as follows:

$$h_k, c_k = H_{cell}(x_k, h_{k-1}, c_{k-1})$$  \hspace{1cm} (1)

where $H_{cell}$ receives the current input $x_k$, the previous hidden $h_{k-1}$, and the previous memory cell $c_{k-1}$. The output will be the updated hidden $h_k$ and cell $c_k$ at the current time step as shown in Fig. 3. The following equations formalize the transition function of the LSTM cell at time step $k$ as

$$i_k = \sigma (V_i x_k + W_i h_{k-1} + b_i)$$  \hspace{1cm} (2)

$$e_k = \sigma (V_e x_k + W_e h_{k-1} + b_e)$$  \hspace{1cm} (3)

$$f_k = \sigma (V_f x_k + W_f h_{k-1} + b_f)$$  \hspace{1cm} (4)

$$g_k = \delta (V_g x_k + W_g h_{k-1} + b_g)$$  \hspace{1cm} (5)

$$c_k = e_k \odot c_{k-1} + i_k \odot g_k$$  \hspace{1cm} (6)

$$h_k = f_k \odot \delta (c_k)$$  \hspace{1cm} (7)
where $\sigma$ and $\delta$ represent nonlinear activation functions of logistic sigmoid and hyperbolic tangent, respectively, $x_S \in \mathbb{R}^M$, $V \in \mathbb{R}^{M \times d}$ and $W_s \in \mathbb{R}^{d \times d}$ are shared model weights. The operator $\odot$ represents the element-wise multiplication.

2) **RUL Prediction Network:** Given the extracted features from the LSTM feature extractor $f_S = E_S(X_S)$. The RUL predictor is a multilayer network $R: \mathbb{R}^d \rightarrow \mathbb{R}$ that maps the latent features into the corresponding RUL value. The RUL predictor $R$ and the feature extractor $E_S$ are trained in an end-to-end manner using the mean square error loss between the predicted RULs and the true RULs, which can be formalized as follows:

$$
L_{mse} = \frac{1}{n_S} \sum_{i=1}^{n_S} (\hat{y}_S^{(i)} - y_S^{(i)})^2
$$

where $\hat{y}_S = R(E_S(X_S))$ is the predicted RUL label, $y_S$ is the ground-truth RUL values, and $n_S$ is the number of source samples.

**D. Contrastive Adversarial Domain Alignment (CADA)**

The contrastive adversarial adaptation module consists of a domain discriminator $D$ and the InfoNCE module as shown in Fig. 4. First, the weights of the trained source feature extractor are adopted to initialize the target feature extractor. The output features from both the source and target domains are fed into an adversarial discriminator network to minimize the discrepancy. Concurrently, the target features are fed into the InfoNCE loss module to preserve the target specific features during the alignment process. In particular, the InfoNCE loss will maximize the mutual information between the target domain inputs and the target domain features to preserve task-specific information. Algorithm 1 shows the formal procedure of our CADA approach. The domain discriminator network that encourages the source and target features to be domain invariant. While the contrastive estimation module maximizes the information between the learned target domain features and the input target domain data to preserve the task-specific features during the adversarial alignment process. Detailed procedures are presented in the following paragraphs.

1) **Adversarial Adaptation Module:** Let $E_S$ and $R_S$ be the source-trained LSTM feature extractor and the RUL predictor, respectively. To predict the RUL labels of the unlabeled target domain data, we naïvely initialize our target model (i.e., $E_T$ and $R_T$) with pretrained source models. However, due to the large discrepancy among the data from different working/fault conditions, the model can fail to predict RUL accurately. To tackle this domain discrepancy problem, we adversarially train the LSTM feature extractor against a domain discriminator network to minimize the distribution differences between the source features and the target features. Specifically, the domain discriminator network $D$ is trained to discern between the source and target features. Concurrently, we train the target feature extractor $E_T$ to produce target features such that the domain discriminator network cannot distinguish them from the source features. The adversarial training between the discriminator network $D$ and the target $E_T$ can be expressed as follows:

$$
\min_{E_T} \max_{D} L_{adv} = E_{X_S \sim P_S} [\log(D(E_S(X_S)))] \\
+ E_{X_T \sim P_T} [\log(1 - D(E_T(X_T)))]
$$

where $X_S$ and $X_T$ are the source and target samples, respectively. The target feature extractor $E_T$ is updated to minimize $L_{adv}$, and the discriminator network $D$ is adversarially trained to maximize $L_{adv}$. Eventually, the trained target feature extractor $E_T$ will be able to extract features $f_T$ that have minimum discrepancy from the source features.

2) **Contrastive Estimation Module:** Adversarial domain adaptation can successfully find target domain features that are invariant from the source features. However, it can remove task-specific information from the target features to minimize the adversarial loss, which can deteriorate the performance on the target domain—even with perfect domain alignment. Hence, it is required to preserve target-specific features during the domain alignment task. To achieve that, we rely on InfoNCE loss [22] to maximize the mutual information between the encoded representations of the target domain and the original inputs, as shown in Algorithm 2. Given a sample $X_T \sim X_T$,
Algorithm 2: Contrastive Loss.

Input: $X_T = \{x_1, \ldots, x_K\}$, $f_T = E_T(X_T)$
Output: Contrastive loss $L_{\text{InfoNCE}}$

$\Theta^k \leftarrow$ Linear layer at timestep $k$

for $K$ timesteps do
1. $q_k \leftarrow \Theta^k f_T$
2. Apply $\phi_k(x_k, q_k^l)$ as in (11)
3. Compute $L_{\text{InfoNCE}}$ using (12)
end
return $L_{\text{InfoNCE}}$

where $X_T \in \mathcal{R}^{M \times K}$, we apply the target encoder $E_T$ on $X_T$ to obtain its corresponding feature representation $f_T = E_T(X_T)$.

To model the mutual information between $x_k$ and $f_T$, following the previous studies [39], we define a density ratio function $\phi_k$ at each time step, which is formalized as follows:

$$\phi_k(x_k; f_T) \propto \frac{p(x_k|f_T)}{p(x_k)}, \quad (10)$$

By maximizing the mutual between the latent target features $f_T$ and the input $x_k$, we can preserve the common latent variables between the target features $f_T$ and the input $x_k$. To compute $\phi_k$, the latent features $f_T$ and the input $x_k$ should be mapped to the same dimension. To achieve that, we use a fully connected network $\Theta : \mathcal{R}^d \rightarrow \mathcal{R}^M$ that maps feature dimension $d$ to input dimension $M$. Thereafter, the density ratio $\phi_k$ is estimated by a dot product between the transformed features $q_k = \Theta^k(f_T)$ and the original input $x_k$, which can be compactly represented as follows:

$$\phi_k(x_k, f_T) = x_k^T q_k \quad (11)$$

where $\Theta^k = \{\theta_1, \ldots, \theta_M\}$ are the weights of a fully connected layer at time step $k$. Note that $\Theta^k$ is different among the time steps.

To maximize the density ratio function, we jointly optimize the target feature extractor $E_T$ and the fully connected layers $\Theta$ using the contrastive estimation loss. The InfoNCE loss maximizes the mutual information by contrasting between the positive and negative samples. Fig. 5 illustrates the positive and negative samples for time step $k = 1$. The overall InfoNCE loss can be formulated as

$$\min_{E_T, \Theta} L_{\text{InfoNCE}} = - \mathbb{E}_{X_T} \left[ \log \frac{e^{\phi_k(x_k, f_T)}}{\sum_{x_{j} \in X_T} e^{\phi_k(x_{j}, f_T)}} \right]. \quad (12)$$

The optimal probability of the NCE loss $p(d = k|X_T, f_T)$ can be formulated as

$$p(d = k|X_T, f_T) = \frac{p(x_k|f_T) \prod_{l \neq k} p(x_l)}{\sum_{j=1}^{K} p(x_j|f_T) \prod_{l \neq j} p(x_l)} \quad (13)$$

By substituting (12) into the aforementioned equations, we can formalize the mutual information in terms of the InfoNCE loss $L_{\text{InfoNCE}}$, detailed derivation can be found in [39]. The resulting formula can be written as

$$I(x_k, f_T) = \log(K) - L_{\text{InfoNCE}} \quad (15)$$

where $I(\cdot)$ represents the mutual information between $x_k$ and $f_T$. It can be seen that minimizing InfoNCE loss is maximizing the lower bound of $I(x_k, f_T)$, which in turn maximizing the mutual information.

3) Overall Loss Function: In this work, the adversarial adaptation loss and contrastive estimation loss are jointly optimized in an end-to-end manner. The total domain alignment loss can be summarized as follows:

$$\min_{E_T, \Theta} \max_{D, \lambda} \mathbb{E}_{X_T \sim p_T} \left[ \log D(f_T) \right] + \mathbb{E}_{X_T \sim p_S} \left[ \log (1 - D(f_T)) - \lambda \log \frac{e^{\phi_k(x_k, f_T)}}{\sum_{x_{j} \in X_T} e^{\phi_k(x_{j}, f_T)}} \right] \quad (16)$$

where $L_{\text{adv}}$ is the adversarial loss, $L_{\text{NCE}}$ is the contrastive estimation loss, and $\lambda$ is a weight parameter that controls the proportion of learning domain-invariant features and preserving task-specific information.

IV. EXPERIMENTS AND RESULTS

A. Preparation of Data

To evaluate the performance of our approach, we employ the popular C-MAPSS [40] benchmark dataset that describes the run-to-fail experiments of aeroengines shown in Fig. 8. It contains four different subsets, namely FD001, FD002, FD003, and FD004, which differ in terms of working conditions, fault modes, life spans, and number of engines, as shown in Table II. Particularly, “# Training engines” represents the number of available engines to train the model, while “# Testing engines” represents the number engines available for testing. “# Training samples” is the total number of training samples per data subset. “# Testing samples” is the total number of testing samples per data subset. “# Max life span” is the maximal number of cycles that an engine takes to go from healthy to the failure condition. “# Operating conditions” represents the number of operating conditions. “# Fault types” represents the number of failure modes occurrblue. Particularly, we take the scenario FD001→FD002 as an example. We use both the training samples of FD001 (17731
Different types of sensors have been used to monitor rotating components of each engine. Here, we briefly introduce our procedure for data processing. First, we select sensors that are informative for RUL prediction, following the previous studies [11], [12]. The informative sensors are those sensors that can show clear degradation trend from run to failure. Here, we visualize the sensor readings of the randomly selected engines. Figs. 6 and 7 show the sensor readings from FD001 and FD002 subsets, respectively. Clearly, some sensors are almost constant during the whole degradation, which can hinder the model from correctly modeling the deterioration process. In the cross-domain problem, we intend to transfer the knowledge from a source data subset (e.g., FD001) to a target data subset (e.g., FD002). Thus, we only select the common sensors among source and target domains that are the most informative ones. Following this strategy, we have selected the following sensors, i.e., S2, S3, S4, S7, S8, S9, S11, S12, S13, S14, S15, S17, S20, and S21.

Second, the same type of sensors may have quite different readings under different working conditions. To reduce the effect of working conditions, we apply the Min–Max normalization with respect to each working condition. As such, the data under different working conditions are normalized into the range of [0,1]. Third, we apply sliding windows to generate data samples from run-to-fail cycles. Following previous studies [11], [12], we set the window size and the step size as 30 and 1, respectively. Moreover, a piece-wise linear RUL [2] is adopted instead of the true RUL, i.e., if the true RUL is larger than the maximal RUL, then it is set to the maximal RUL.

### B. Experimental Settings

Our CADA approach consists of the following five main models: Source feature extractor ($E_S$), target feature extractor ($E_T$), RUL predictor ($R$), domain discriminator ($D$), and InfoNCE module. A detailed structure of each model has been shown in Fig. 4. Specifically, the source and target feature extractors are deep BiLSTM networks with five layers, where each layer has 32 neurons. The discriminator is composed of three fully connected (FC) layers with 64, 32, and 1 hidden neurons. The RUL predictor also consists of three FC layers, i.e., hidden layer 1 with 32 neurons, hidden layer 2 with 16 neurons, and output layer with a single neuron. Each layer is followed by a nonlinear activation function called rectified linear unit (ReLU) and the dropout regularization technique to relieve the overfitting problem. The detailed architecture of the RUL predictor is shown in Fig. 9.

To train our model, we adopt the minibatch training with a batch size of 256. To reduce overfitting, dropout regularization is adopted across the whole structure and the dropout ratio is set to be 0.5. We use an Adam optimizer to minimize the joint loss with the learning rate of 0.5e-4 for the feature extractor and the domain discriminator. As the InfoNCE module is trained from...
TABLE III
COMPARISON OF THE PROPOSED METHOD AGAINST STATE-OF-THE-ART APPROACHES

<table>
<thead>
<tr>
<th>Metric</th>
<th>RMSE</th>
<th>Score</th>
</tr>
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<tbody>
<tr>
<td>FD001→FD002</td>
<td>22.83</td>
<td>31.14</td>
</tr>
<tr>
<td>FD001→FD003</td>
<td>44.21</td>
<td>71.77</td>
</tr>
<tr>
<td>FD001→FD004</td>
<td>50.03</td>
<td>57.41</td>
</tr>
<tr>
<td>FD001→FD001</td>
<td>24.43</td>
<td>35.24</td>
</tr>
<tr>
<td>FD002→FD003</td>
<td>42.86</td>
<td>61.45</td>
</tr>
<tr>
<td>FD002→FD004</td>
<td>22.12</td>
<td>57.87</td>
</tr>
<tr>
<td>FD003→FD001</td>
<td>40.33</td>
<td>56.05</td>
</tr>
<tr>
<td>FD003→FD002</td>
<td>56.87</td>
<td>60.11</td>
</tr>
<tr>
<td>FD003→FD004</td>
<td>58.16</td>
<td>29.44</td>
</tr>
<tr>
<td>FD004→FD001</td>
<td>51.44</td>
<td>42.01</td>
</tr>
<tr>
<td>FD004→FD002</td>
<td>31.81</td>
<td>35.88</td>
</tr>
<tr>
<td>FD004→FD003</td>
<td>30.44</td>
<td>19.14</td>
</tr>
</tbody>
</table>

The bold entities represent the best performance among each cross-domain scenario.

C. Comparison With State-of-the-Art Methods

To evaluate our approach in cross-domain scenarios, we train the model using a labeled source domain (e.g., FD001) and evaluate on an unlabeled target domain (e.g., FD002, FD003, or FD004). As we have four subdatasets (i.e., domains), we thus have 12 cross-domain scenarios. In this article, we implement five state-of-the-art approaches as follows. In addition, we report the average performance (i.e., RMSE and Score) over five consecutive runs with different random seeds.

1) Correlation alignment (CORAL) [26]: CORAL minimizes the covariance shift between the source and target features to align the distribution.

2) Deep domain confusion (DDC) [25]: DDC employs a distance metric called MMD to confuse the source and target features.

3) Wasserstein distance guided representation learning (WDGLR) [41]: WDGLR employs a neural network to measure the empirical Wasserstein distance, while utilizing the feature extractor network to minimize this distance between the source and target domain.

4) Adversarial discriminative domain adaptation (ADDA) [28]: ADDA uses a typical GAN loss to find target domain features that can be similar to the source features.

5) Deep domain adaptation (DDARUL) [14]: In DDARUL, an LSTM feature extractor is trained to confuse the source and target domains, while a domain classifier network is trained to classify between the source and target features.

Table III shows the experimental results. The CADA outperforms all the competing approaches across the 12 cross-domain scenarios in terms of both RMSE and Score. In addition, we observe that knowledge transfer between simple and complex datasets is challenging due to the large domain shift, yet our CADA can successfully align the two distant domains. For example, FD001 and FD004 are the simplest and most complex data subsets, respectively. As shown in Table III, simply forcing the features to be similar among these two datasets can significantly harm the performance. Overall, we achieve significant improvement over the second best approach (underlined) in

Fig. 9. Detailed architecture of the RUL predictor network.
TABLE IV
ABLATION STUDY OF THE PROPOSED APPROACH

<table>
<thead>
<tr>
<th>Metric</th>
<th>RMSE</th>
<th>Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>Method</td>
<td>Source-Only</td>
<td>w/o InfoNCE</td>
</tr>
<tr>
<td>FD01→FD001</td>
<td>20.82</td>
<td>19.52</td>
</tr>
<tr>
<td>FD01→FD003</td>
<td>35.09</td>
<td>33.53</td>
</tr>
<tr>
<td>FD01→FD004</td>
<td>34.83</td>
<td>32.19</td>
</tr>
<tr>
<td>FD02→FD001</td>
<td>15.29</td>
<td>14.82</td>
</tr>
<tr>
<td>FD02→FD003</td>
<td>35.46</td>
<td>33.65</td>
</tr>
<tr>
<td>FD02→FD004</td>
<td>37.64</td>
<td>35.42</td>
</tr>
<tr>
<td>FD02→FD001</td>
<td>39.03</td>
<td>24.66</td>
</tr>
<tr>
<td>FD02→FD002</td>
<td>46.11</td>
<td>24.86</td>
</tr>
<tr>
<td>FD02→FD004</td>
<td>51.64</td>
<td>21.94</td>
</tr>
<tr>
<td>FD04→FD001</td>
<td>57.90</td>
<td>26.34</td>
</tr>
<tr>
<td>FD04→FD002</td>
<td>32.98</td>
<td>28.73</td>
</tr>
<tr>
<td>FD04→FD003</td>
<td>19.47</td>
<td>14.38</td>
</tr>
</tbody>
</table>

The bold entities represent the best performance among each cross-domain scenario.

Fig. 10. Experimental results with different λ values for 12 cross-domain scenarios.

TABLE V
VALUES OF λ AND THE NUMBER OF LSTM LAYERS FOR DIFFERENT SCENARIOS

<table>
<thead>
<tr>
<th>Scenario</th>
<th>λ</th>
<th>Number of Layers</th>
</tr>
</thead>
<tbody>
<tr>
<td>FD01→FD002</td>
<td>0.2</td>
<td>5</td>
</tr>
<tr>
<td>FD01→FD003</td>
<td>0.2</td>
<td>3</td>
</tr>
<tr>
<td>FD01→FD004</td>
<td>0.001</td>
<td>5</td>
</tr>
<tr>
<td>FD02→FD001</td>
<td>0.001</td>
<td>5</td>
</tr>
<tr>
<td>FD02→FD003</td>
<td>0.001</td>
<td>5</td>
</tr>
<tr>
<td>FD02→FD004</td>
<td>0.001</td>
<td>5</td>
</tr>
<tr>
<td>FD03→FD001</td>
<td>0.5</td>
<td>5</td>
</tr>
<tr>
<td>FD03→FD002</td>
<td>0.5</td>
<td>5</td>
</tr>
<tr>
<td>FD03→FD004</td>
<td>0.2</td>
<td>3</td>
</tr>
<tr>
<td>FD04→FD001</td>
<td>0.2</td>
<td>3</td>
</tr>
<tr>
<td>FD04→FD002</td>
<td>0.2</td>
<td>5</td>
</tr>
<tr>
<td>FD04→FD003</td>
<td>0.001</td>
<td>1</td>
</tr>
</tbody>
</table>

Fig. 11. Experimental results with different number of LSTM layers for 12 cross-domain scenarios.

D. Model Ablation Study

Here, we perform our ablation study to verify the contribution of individual components in our CADA approach. We derive two variants of CADA, namely, “Source-Only” and “w/o InfoNCE”. In particular, “Source-Only” refers to the nonadapted version of our model, whereas the “w/o InfoNCE” is our adversarial adaptation approach without using the contrastive estimation loss.

Table IV shows the comparison between the CADA and its two variants. We observe that the “Source-Only” has the worst performance, indicating that the big gap between the source and target domain data distributions. The proposed CADA method outperforms the one without the InfoNCE loss in most of cases, which signifies the effectiveness of the InfoNCE loss on domain adaptation-based RUL prediction.

E. Sensitivity Analysis

1) Coefficient of the InfoNCE Loss λ: In this section, we investigate the sensitivity of the proposed CADA with respect to the coefficient of the InfoNCE loss λ. We have conducted experiments with λ varying from 0.001 to 1.0 for the 12 cross-domain scenarios. The results are shown in Fig. 10. It can be found that different scenarios may require different λ to boost the performance. Table V summarizes the selected λ values for the 12 cross-domain scenarios in experiments.

2) Number of LSTM Layers: Another important hyperparameter for the proposed method is the number of LSTM layers.
We have investigated the model performance with different numbers of LSTM layers, i.e., 1, 3, 5, and 7, in order to find a balance between the model performance and the training time. Fig. 11 shows the experimental results. We can find that the proposed method with five layers can achieve the best performance in most of the scenarios. However, some scenarios require fewer layers to obtain a better or comparable performance. For example, for the scenario FD004->FD003, the method with seven LSTM layers performs the best. However, the performance of the method with one LSTM layer is comparable to the best performance, but much more efficient. In this case, using a single LSTM layer is more reasonable when considering the balance between the performance and the efficiency of the algorithm. Table V shows the selected number of LSTM layers for each cross-domain scenario.

V. CONCLUSION

In this article, we proposed a novel CADA approach that can automatically find domain-invariant features while preserving domain-specific information for the machine RUL prediction. The proposed CADA method was built upon the adversarial domain adaptation architecture with the novel InfoNCE loss. We performed extensive experiments to verify the effectiveness of the CADA method. More specifically, a detailed comparison was made with five state-of-the-art approaches for domain adaptation in RUL prediction. Our experimental results showed that the proposed CADA method significantly outperforms all the state-of-the-arts. Moreover, we also conducted ablation study to show the effectiveness of the InfoNCE loss when performing domain adaptation.

REFERENCES

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